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CHARGE TRANSPORT IN BOTTOM-UP INORGANIC-ORGANIC AND QUANTUM-COHERENT NANOSTRUCTURES

on Friday, 22nd of May, 2015 at 12:45

in the Prof. Dr. G. Berkhoff-zaal,
Waaier building,
University of Twente

Prior to the defence at 12:30
I will give a brief introduction to the thesis

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QUANTUM-COHERENT NANOSTRUCTURES
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DISSERTATION

to obtain
the degree of doctor at the University of Twente,
on the authority of the rector magnificus,
prof. dr. H. Brinksma,
on account of the decision of the graduation committee,
to be publicly defended
on Friday 22 May 2015 at 12.45

by

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born on 11th February 1987
in Taganrog, USSR
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Printed in The Netherlands, 2015
... to my family...

...моей семье ...
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Chapter 1 INTRODUCTION

“An Experiment, like every other event which takes place, is a natural phenomenon; but in a Scientific Experiment the circumstances are so arranged that the relations between a particular set of phenomena may be studied to the best advantage”.

James Clerk Maxwell, 1876
Chapter 1

The semiconductor electronics industry is showing a dramatic downscaling of the size of electronic devices driven by scientific and technological innovations [1]. If this scaling continues down to one molecule as an individual logic or memory unit hybrid electronics (where inorganic and organic molecular materials are combined [2]), in an irrevocable connection with quantum-mechanical phenomena (usually coming into view at nanoscale and at the temperatures close to absolute zero), could play a major role for the future of electronics. In fact, the potential of molecular electronics for applications such as diodes and memories has already been demonstrated [3].

The relatively young field of mesoscopic physics forms a bridge between the macroscopic world of bulk materials and the microscopic world of atoms and molecules and explores semiconducting, metallic and superconducting systems with typical dimensions in the range of 0.01-10 µm. Mesoscopic physics is interested in a big variety of questions. What is a boundary condition of the size of a piece of material that “averages away” the wave-nature of a particle, governed by quantum mechanics, and “recover” its classical behaviour? If there are only a few electrons available, how will they behave? And many more...

“It seems as though we must use sometimes the one theory and sometimes the other, while at times we may use either. We are faced with a new kind of difficulty. We have two contradictory pictures of reality; separately neither of them fully explains the phenomena of light, but together they do"

Albert Einstein and Leopold Infeld, 1938

In this thesis, we use diffusive systems as inorganic components (Au films, Au nanorods (NRs) and Au nanoparticles (NPs)), and self-assembled molecular layers as organic part in order to build hybrid devices. Chapter 1 gives a brief introduction to the charge transport through molecular layers and to the main phenomena in the diffusive regime. These are the Aharonov-Bohm (AB) effect, universal conductance fluctuations (UCF), and the Coulomb blockade which reveal the quantum and classical behaviour of electrons. Chapter 1 also describes experimental methods and techniques required to open the secrets of electron transport. Chapters 2-3 are dedicated to the two different methods (dielectrophoresis and wedging transfer techniques, respectively) of the molecular junction fabrication and the consistent study of the charge transport mechanisms through organic molecular layers. A unique bottom-up approach of the fabrication of single-electron transistors (SETs) is described in detail in chapter 4, followed by the investigation of the electron
behaviour in a pair of metallic Coulomb islands coupled via molecular barriers in parallel (Chapter 5). Chapter 6 discusses dynamic nonlocality in a diffusive system where AB effect is used as a switch to tune electron transport. In the end of the thesis (Chapter 7) we show an indication of the coherent electron transport in a hybrid inorganic-organic AB interferometer with embedded molecular junctions and propose novel geometries of hybrid AB rings for future studies of the coherence in organic molecules.

1.1. Aharonov-Bohm Effect

In 1959, Yakir Aharonov and David Joseph Bohm formulated a Gedanken Experiment describing how a magnetic flux affects the interference of a split electron wave (Fig. 1.1) [4]. They suggested that if a single-electron wave is split into two partial waves enclosing a flux localised in the area between the two waves, such that no magnetic field $B \text{ exists anywhere along the path of the electron wave}$, the vector potential $A$ associated with field cannot be taken equal to zero and still effects the phase of the electron wave. Similarly, an electrostatic potential $V$ contributes to the phase even in absence of an electric field $E$.

![Figure 1.1. Schematic experiment to demonstrate single-electron interference with a time-independent magnetic vector-potential [4].](image)

The phase $\varphi$ acquired by the electron wave, while travelling along the path, is given by:

$$\varphi = \frac{2\pi}{\hbar} \int (mv + |e| A) \cdot ds = 2\pi \frac{|e|}{\hbar} \left[ \int V dt + \int A \cdot ds \right], \quad (1.1)$$

where $\hbar$ is the Planck constant, $e$ is the elementary charge, $s$ is a completed path and $m$ and $v$ are electron mass and velocity, respectively. The phase difference between the two paths is:

$$\Delta \varphi = \varphi_1 - \varphi_2 = 2\pi \frac{|e|}{\hbar} \left[ \int_0^t \Delta V dt + \oint \vec{A} \cdot d\vec{l} \right] = 2\pi \frac{|e|}{\hbar} \Delta V t_0 + 2\pi \frac{|e|}{\hbar} BS, \quad (1.2)$$
\[ \Delta \phi_{\Delta V} = 2\pi \frac{|e|}{h} \Delta V t_0, \quad (1.3) \]

\[ \Delta \phi_A = 2\pi \frac{|e|}{h} BS, \quad (1.4) \]

where \( \Delta V \) is the electrostatic potential difference between two paths, \( t_0 \) is the time between splitting and recombination of the single-electron wave, \( S \) is the enclosed area by two paths, \( \Delta \phi_{\Delta V} \) and \( \Delta \phi_A \) are contributions to the phase difference by the electrostatic and magnetic potentials, respectively. The first experimental observation of the Aharonov-Bohm effect in a single diffusive metal ring was performed in 1985 by Webb et al [5]. The importance of the AB effect is underlined by the qualification "one of the seven wonders of the quantum world" by the New Scientist magazine [6].

1.2. Universal Conductance Fluctuations

Universal conductance fluctuations are observed in coherent mesoscopic systems during electrical measurements at low temperatures and originated from a magnetic flux, piercing the leads in the device [7-9]. The physical origin of UCF is the same as of the AB effect, interference. Due to the artificially fixed geometry of the path, which electron wave function takes in a AB interferometer, AB signal has a periodic character in magnetic field with a period of \( \Delta B = h/|e|S \) (Eq.1.4) (where \( n \) is a harmonic number). While UCF take place in the wires and leads of the device, where there is no well-defined AB path, so that the correlated field is limited by the size of the device and the coherence length. Therefore, the effect is rather random leading to the appearance of the aperiodic fluctuations. UCF will appear in any (semi-)conducting systems independent of the sample size and degree of disorder [7], when the \( B \)-field goes through the device.

AB effect and UCF are governed by a magnetic flux penetrating the device and magnitudes of their fluctuations are both in the order of \( e^2/h \). The period of AB oscillations is determined by the ring’s enclosed area \( S_{in} \), while UCF are correlated with the area of the arms \( S_{arm} \). This leads to the fact that in order to distinguish AB effect from UCF the aspect ratio between \( S_{in} \) and \( S_{arm} \) should be \( \gg 1 \).

1.3. Coulomb Blockade

A Coulomb island is an isolated conductor that can be filled with electrons and perform single-electron transport (Fig. 1.2a) [10]. Coulomb islands have been shown to be useful systems to study a wide range of physical phenomena. In the following experiments we are using citrate (Chapter 2) and
cetyltrimethylammonium bromide stabilized (Chapters 4,5) Au nanoparticles (NPs) with a diameter of 20 nm as Coulomb islands.

By applying small voltages at low temperatures it is possible to observe **Coulomb blockade**, an important phenomenon of the suppressed conductance through the Coulomb island. Figure 1.2a shows a schematic of the confined Coulomb island coupled via tunnel barriers to the three terminals: source, drain and gate electrodes. Source and drain provide a voltage drop across the Coulomb island resulting in the staircase current-voltage characteristic while the gate serves to change its electrostatic energy giving rise to the **Coulomb oscillations** in the current-voltage spectrum.

![Figure 1.2. Schematics of (a) a confined Coulomb island and (b) electrochemical potentials \( \mu_{\text{dot}}(N) \) in an island showing single-electron transport. \( R_s \) and \( R_d \) are tunnel resistances through source and drain, respectively.](image)

The total number of electrons residing on the island is \( N e \) (where \( e \) is the elementary charge and \( N \) is an integer number). When tunnelling occurs, the charge of the island changes by \( e \). An addition of one elementary charge on the object will require a charging energy of \( E_C = e^2 / C \), where \( C \) is the capacitance of the island. This capacitance is the sum of the capacitances between the dot and source \( C_s \), drain \( C_d \) and gate \( C_g \): \( C = C_s + C_d + C_g \). Charging energy becomes important when it dominates over the thermal energy \( k_B T \) (where \( k_B \) is the Boltzmann constant and \( T \) is the temperature), and when barriers are sufficiently opaque such that electrons are located either in the source, in the drain, or on the island. Typical time to charge/discharge an island is \( \Delta t = R_t C \), where \( R_t \) is tunnel resistance of the barriers. From the Heisenberg uncertainty principle \( E \Delta t = (e^2 / C) R_t C > h \) (where \( h \) is the Planck constant) follows [11]:

\[
R_t \gg h/e^2, \tag{1.5}
\]
\[ e^2/C \gg k_B T \] (1.6)

The current through the Coulomb island is determined by the number of available states on the island that follows from the calculation of its electrochemical potential \( \mu_{\text{dot}}(N) \). This is by definition the minimum energy to add one electron to an island:

\[
\mu_{\text{dot}}(N) \equiv U(N) - U(N - 1) = E_N + \frac{(N-N_0-1/2)e^2}{C} - e \frac{C_g}{C} V_{\text{gate}},
\] (1.7)

where \( U(N) \) is the total ground state energy for \( N \) electrons on the island at zero temperature and at a gate voltage \( V_{\text{gate}} \), \( N_0 \) is the number of electrons at zero gate voltage, \( E_N \) represents the chemical contribution \( \mu_{\text{ch}}(N) \). Electron transport through the island is possible only when \( \mu_{\text{dot}}(N) \) lies between electrochemical potentials of the source \( \mu_{\text{left}} \) and drain \( \mu_{\text{right}} \): \( \mu_{\text{left}} \geq \mu_{\text{dot}} \geq \mu_{\text{right}} \) (Fig. 1.2b). When at fixed gate voltage, the number of electrons is changed by one, the resulting change in electrochemical potential is:

\[
\Delta \mu_{\text{dot}}(N) = \mu_{\text{dot}}(N + 1) - \mu_{\text{dot}}(N) = E_C + \Delta E,
\] (1.8)

where \( \Delta E \) is the energy spacing between two discrete quantum levels.

Figure 1.3 shows a schematic stability diagram (Coulomb diamonds) of the electron transport through the Coulomb island as a function of the source-drain voltage \( V_{\text{bias}} \) and \( V_{\text{gate}} \), where grey areas represent the suppressed conduction through the island.

![Stability Diagram](image)

**Figure 1.3.** Stability diagram showing single-electron transport through the Coulomb island as a function of \( V_{\text{bias}} \) and \( V_{\text{gate}} \), where grey areas represent the suppressed conduction through the island. From the slopes of the Coulomb diamonds important coupling parameters can be extracted.
In the regime that thermal broadening $k_B T$ is greater than tunnelling broadening $h\Gamma$ (where $\Gamma = I/e$ is tunnelling rate and $I$ is the total current through barriers) [11], Coulomb blockade can be divided into two thermal regimes determined by the spacing between energy levels $\Delta E$ on the Coulomb island: classical (or metallic), when many levels are excited by thermal fluctuations ($\Delta E \ll k_B T \ll e^2/C$), or quantum, when only one or a few levels participate in transport ($k_B T \ll \Delta E \ll e^2/C$) [11].

![Figure 1.4. Calculated temperature dependence of the Coulomb oscillations as a function of Fermi energy in the classical regime. The parameters are $\Delta E = 0.01e^2/C$ and $k_B T/(e^2/C) = 0.075$ [a], 0.15 [b], 0.3 [c], 0.4 [d], 1 [e], and 2 [f] [12].](image)

The classical Coulomb blockade regime can be described by the so-called “orthodox” theory [13, 14], and the calculated temperature dependence of the Coulomb oscillations is shown in Fig. 1.4a, where the shape of an individual Coulomb peak is described by:

$$\frac{G}{G_\infty} = \frac{1}{2} \cosh^{-2} \left( \frac{e(C_g-C)\left| V_{\text{gate, res}} - V_{\text{gate}} \right|}{2.5k_B T} \right)$$

where $G$ is the conductance through the Coulomb island, $G_\infty$ is the conductance through the barriers at high temperature and $V_{\text{gate, res}}$ is the gate voltage at the resonance.
1.4. Charge Transport Through Organic Molecules

Two most prevalent transport mechanisms through molecular junctions are known and well-studied: coherent non-resonant tunnelling, which dominates in short molecules, and incoherent charge hopping, mostly observed in long-conjugated molecular wires [15-17]. In this thesis we focused on molecular self-assembled monolayers (SAMs) of alkenes and $\pi$-conjugated molecules, where transport is generally driven by a non-resonant tunnelling [18].

The molecules can vary in length, structure, packing and bonding group. In this thesis we chose alkanedithiols, oligo(phenylene vinylene) (OPV) and oligo(phenylene ethynylene) (OPE) (Sigma-Aldrich) (Fig. 1.5). Due to a smaller band gap between the highest occupied (HOMO) and lowest unoccupied (LUMO) molecular orbitals (also known as frontier orbitals) $\pi$-conjugated molecules are, in general, better conductors than alkenes [19]. Nevertheless, the local environment and the way the molecules are contacted can resolve whether tunnelling or hopping transport mechanism dominates for OPEs [20].

![Figure 1.5. Examples of the molecules of interest. a-c, alkanedithiols containing five (a), six (b) and nine (c) carbons; (d), OPV2; (e), OPE3.](image)

Due to a big HOMO-LUMO gap (e.g., $\sim$8 eV for alkyl systems) [21], molecular SAMs embedded between metallic electrodes represent a simple classical molecular junction (Fig. 1.6). Depending on the molecule's characteristics as well as on the metal work function, the distance between Fermi level and closest molecular level can vary. Simons' approximation can
be used to model the current-voltage behaviour of a molecular junction acting as a tunnel barrier [22].

![Energy band diagram of a molecular junction at zero bias voltage, where $E_F$ is a Fermi energy of the electrodes.](image1)

**Figure 1.6.** Energy band diagram of a molecular junction at zero bias voltage, where $E_F$ is a Fermi energy of the electrodes.

The coherent tunnelling process is temperature-independent and the resistance ($R$) through the molecular layer exponentially increases with increasing molecular chain length:

$$ R = R_0 e^{(\beta d)} $$

(1.10)

where $R_0$ is an effective contact resistance that depends on the anchoring group and contact electrodes; and $\beta$ is the tunnelling decay factor that depends on the nature of the molecular structure and applied voltage [16, 23]. More details about the coherent non-resonant tunnelling can be found in Ref. [21].

![Energy band diagram of a molecular tunnelling junction showing elastic and inelastic tunnelling. Inelastic tunnelling is accompanied by the energy loss/gain. $E_F$ is the Fermi energy of the electrodes.](image2)

**Figure 1.7.** Energy band diagram of a molecular tunnelling junction showing elastic and inelastic tunnelling. Inelastic tunnelling is accompanied by the energy loss/gain. $E_F$ is the Fermi energy of the electrodes.
When under applied bias voltage (Fig. 1.7) an electron tunnels through the molecular junction and its energy is preserved, the process is elastic, thus, coherent tunnelling. Any inelastic event involving energy exchange leads to the incoherent transport through the molecular layer [24].

1.5. Sample Fabrication and Measurements Techniques

“Experimental physics cannot do without instruments...”

Jean-Antoine Nollet, 1770

Different techniques and equipment were utilized to fabricate, electrically characterise and analyse all the devices described in this thesis. For the sample fabrication, optical lithography, electron beam lithography (EBL) and electron beam metal evaporation were used. Primary sample characterisation was performed by scanning electron microscopy (SEM) and/or atomic force microscopy (AFM) imaging. Room temperature measurements in high vacuum (∼10⁻⁵ mbar) were performed in a probe station followed, if needed, by low temperature measurements in a closed-cycle cryostat or in a cryogen free dilution refrigerator.

Advantages of contact optical lithography are low cost, high throughput and moderately high resolution (limited by the wavelength of light). This technique was utilized to prepare large-area (e.g., 100×100 µm²) electrical contacts where high resolution (<1 µm) is not an issue.

EBL is a high-cost technique with low throughput. The main advantage of EBL is a very high resolution. EBL was used only for the fabrication of the most crucial parts of the devices. Sub-20 nm structures were obtained in this thesis using this technique.

1.5.1. Processing Details

Four-inch p++ Si (100) (0.010-0.025 Ω·cm) wafers with a thermally grown 35 nm SiO₂ (Electronics UCL) were used as substrates in all experiments. A highly boron-doped Si substrate underneath the thin oxide layer can be used as a back gate during electrical characterisation.

Prior to the deposition of resists, the wafers were diced into 11x11 mm² samples (Dicing saw Disco DAD 321) and then properly cleaned in acetone and isopropanol in a sonication bath followed by the spin-coating of
polymethylmethacrylate (PMMA 950 A2 or PMMA 950 A4) resist (spun for 1 min at 1500 and 4000 rpm for PMMA 950 A2 and A4, respectively). Afterwards, samples were baked at 160 °C for 2 min using a hot plate or left over night in the wet-bench for degassing.

For the EBL patterning, we employed a Raith 150 TWO (Raith GmbH) system equipped with a thermal field-emission cathode and a laser interferometer stage. The EBL system was operated at 20 kV and with electron beam currents of 36 pA and 1.2 nA for high and low resolution structures, respectively. All structures were exposed in a writing field of 100×100 μm² with a step size 2 or 26 nm.

Following the EBL exposure, the resist was developed in a mixture of methylisobutylketone/isopropanol (MIBK/IPA 1:3) for 30 sec, the wafers were rinsed in isopropanol and blown dry with nitrogen. Immediately after development, the resist residuals were ashed in O₂ plasma for 20 s at 300 W with 18 % O₂ flow (Tepla 300E O₂ plasma etcher) or removed by ozone cleaning for 5 min (Ozone UV PRS 100 reactor). Following the cleaning procedure, a metal film (Au or Ti/Au) was evaporated in the metal evaporator (BAK 600) with an evaporation rate ≥ 2 Å/s and lifted-off in acetone.

A mask aligner EVG 620 with robot was employed for the optical lithography patterning. Prior to the exposure, primer hexamethyldisilazane (HMDS) was spin-coated for 30 s at 4000 rpm followed by deposition of the photoresist 907/17 for 30 sec at 4000 rpm. After prebaking for 1 min at 95 °C, samples were exposed for 4 s. Following the exposure, the samples were developed in OPD 4262 (an aqueous solution of tetramethylammonium hydroxide (TMAH) at 2.5 %) for 60 s, rinsed in deionized water and spun dry with nitrogen blow. After the resist residuals removal and metal film evaporation, it was lifted-off in acetone.

A SEM FEI Sirion HR-SEM, a FEI Focused Ion Beam System (FIB) with a dual beam or Zeiss MERLIN HR-SEM were used for the detailed surface studies of the fabricated samples. Typically, the accelerating voltage of the SEM was 5 kV, and the working distance was varying from 6 to 10 mm.

For the AFM imaging, a Bruker ICON was employed when it was crucial to avoid any contamination (especially by carbon deposition due to the SEM imaging). The Bruker ICON AFM also allows to perform automatic imaging.

Primary electrical characterisation of the fabricated devices was performed in a probe station (Janis ST-500) with a two-wire configuration using Beep-R, a source-meter that can quickly probe the resistance by applying a maximum voltage drop of 10 mV, and/or Keithley 2400.
SourceMeter controlled by a homemade LabView based program with an a
typical applied voltage of 10 mV (up to 1 V was applied to study electron
transport through molecular junctions). The probe station Janis ST-500 allows
us to perform measurements in vacuum (\(\sim 10^{-5}\) mbar), and between 4 K and
475 K.

Low-temperature and magnetoresistance measurements were carried
out in a closed-cycle cryostat (Oxford Instruments Heliox VL) with a base
temperature of 230 mK (maximum hold time of 70 hours and a
superconducting magnet with a maximum field of \(\pm 8\) T) or in a cryogen free
dilution refrigerator (Oxford Instruments Triton\textsuperscript{TM}200) with a base
temperature of 7 mK and a vector magnet that can reach \(\pm 6\) T in the \(z\)-
direction and \(\pm 1\) T in \(x\)- and \(y\)-directions.

In order to improve signal-to-noise ratio a lock-in amplifier (Stanford
Research Systems SR830) in combination with IVVI-DAC rack (Quantum
Transport designed instrumentation, TU Delft, design by Ing. Raymond
Schouten).

In the following experiments we used homocysteine (>95%, Sigma-
Aldrich), cetyltrimethylammonium bromide (CTAB) (99%, Aldrich), Au NRs
(Nanopartz, OD=1). MiliQ water was used for all solution preparations and
experiments.

1.5.2. Deposition of Self-Assembled Monolayers

In our experiments we fabricated different devices of a diverse geometry and
performance (such as AB rings, SETs based on Au NRs and NPs) which have
been functionalised by self-assembled monolayers (SAMs). Functionalisation
was performed by immersing samples into a dilute solution of desired
molecules. Typical concentration was 5 mM [25]. Alkeindithiols were
dissolved in ethanol, while THF (tetrahydrofuran) was used for OPV2 and
OPE3 molecules. Samples were ready for further experimentation after 24-48
hours and afterwards cleaned with solvent only and blown dry with nitrogen.

1.6. Electrical Contacting of Nano Objects by Electron Beam
Lithography

1.6.1. Bitmap Markers Formation

When nano objects, randomly placed on the substrate, have to be electrically
contacted by EBL, it is crucial to determine the exact location of the nano
objects of interest (Chapter 4). In this work we used a 1.5×1.5 mm\(^2\) area in the
middle of the 11×11 mm^2 Si/SiO_2 samples to pre-pattern the substrate with a bitmap and four global marks to perform rough alignment. This 1.5×1.5 mm^2 space area was divided into 100×100 mm^2 writing fields and numbered from A to O in the x-direction and from 1 to 15 in the y-direction (Fig. 1.8a). Every 100×100 µm^2 field (Fig. 1.8b) contains four local alignment markers, which are simple crosses (Fig. 1.8c), and hundred bitmap markers in the middle of the writing field. Each bitmap marker is a unique combination of 100×100 nm^2 squares (e.g. in Fig. 1.8d) with a separation between two neighbouring bitmap markers of 4 µm.

![Figure 1.8](image.png)

**Figure 1.8.** EBL design of the pre-patterned substrate. b, 100×100 µm^2 writing field, containing alignment (green, c) and bitmap (blue, d) markers, where red areas (c) are used for the automatic alignment between different pattern layers.

The metal thickness of the bitmap and alignment markers has to be chosen such that it gives a good contrast during imaging (when we find the location of an interesting nano object and perform the alignment) and at the
same time should not be too thick which can give problems during the deposition of contacting electrodes. In our experiments we chose a 3/30 nm Ti/Au double metal layer. Figure 1.9 shows a SEM image demonstrating a part of the bitmap with a zoom-in of one of the markers (in the inset). Since every bitmap marker is unique within one writing field we can determine the location of a nano object of interest with a precision limited by atomic force microscopy imaging.

![Figure 1.9. SEM image of a Ti/Au bitmap markers on top of Si/SiO₂ substrate used for the identification of NR-NP-NR assemblies deposited afterwards (inset shows a zoom-in of one of the markers).](image)

1.6.2. **Top-Down Electrical Contacting**

Following bottom-up formation of NR-NP-NR assemblies (Chapter 4) we fabricated electrical contacts by EBL with a precision better than 20 nm. Our experiments have shown that prebaking of the resist resulted in a formation of short contacts between NRs and NPs. To avoid this, samples were left over night for the degassing on a wet bench protected on top by the glass beaker and with a nitrogen flow access. Afterwards, an EBL procedure was performed.

Another crucial step is SEM imaging. We observed formation of a thick contamination layer in exposed areas. Figure 1.10a shows AFM image of the contacted NRs-MPs-NRs assembly which has been SEM imaged before (Fig. 1.10b). Scanning with electron beam formed a contamination layer of about 5
nm (Fig. 1.10c). This dramatically influences the performance of the fabricated devices. Particularly, the formed contamination layer between assemblies and electrical contacts is insulating and results in open circuit.

**Figure 1.10.** a, AFM image of the contacted self-assembled NR-NP structure (defined by blue and red, respectively, in b) after SEM imaging of the high-lighted by yellow dashed line area (b) showing about 5 nm thick carbon layer (c).

1.7. Design of Aharonov-Bohm Interferometers

Quantum-mechanical phenomena like AB effect can be observed when electrons preserve their phase, i.e. \( l_e < l_\phi \sim L \) (where \( l_e \) is the elastic scattering length, \( l_\phi \) is the phase coherence or inelastic scattering length, and \( L \) is the system size, more specifically the length of the circumference of the AB ring) [26]. This condition can be achieved by performing the measurements at low temperature (~1 K).

In order to distinguish the AB effect from UCF the aspect ratio between \( S_{in} \) and \( S_{arm} \) should be \( \gg 1 \) (Section 1.2). As a result, an AB ring should be carefully designed. Figure 1.11 shows a typical AB interferometer studied in this thesis.
1.8. Low Noise Measurements

The Coulomb blockade effect can be observed when the charging energy (the energy that is required to charge the Coulomb island with one elementary charge) is larger than the thermal energy of an electron. It can often be achieved by performing charge transport measurements at low temperatures. Depending on the size of the Coulomb island, the effect can generally be observed below liquid nitrogen temperature \[27\].

In order to observe quantum coherent effects, like the AB effect, the coherent length \( l_\phi \) should be long enough \( (l_\phi \sim L) \) [28]. Therefore, it is necessary to cool down devices to milliKelvin temperatures (<1 K) where phonon excitations are minimized [29]. Thereby, the thermal energy at certain temperature \( T \) limits the excitation current/applied voltage \( (I \sim eV \ll 3.5k_BT) \) [30], and examples are given in Table 1.1. Since the amplitude of the AB oscillations is generally in order of \( \approx 1\% \) of the main signal \( (\Delta I(\Delta V) \approx 0.01I(V)) \), noise and interference reduction in electrical measurement setup becomes crucial and is somewhat of an art.

Another factor limiting the resolution of the electric signal measured across molecular junctions is high resistance of devices \( (I = V/R) \). The resistance of molecular junctions studied in this work and embedded in hybrid inorganic-organic AB interferometers varies between hundreds of kiloOhms and hundreds of GigaOhms. Nevertheless, the resolution of the measurements of the sample resistance \( R \) is limited by the cut-off frequency \( f_c \)
due to the capacitances $C$ (which are in order of nanoFarad) in filters in the measurement system:

$$f_c = \frac{1}{2\pi RC} \rightarrow R_{\text{max}} = \frac{1}{2\pi f_c C} \approx \frac{0.2 \times 10^9}{f_c} = 2 \text{ MΩ}, \text{ (for } f_c = 100 \text{ Hz) \ (1.11)}$$

Noise is caused by a large number of processes; each of them has very small magnitudes. Johnson noise, shot noise and $1/f$ noise contribute the overall noise level. Johnson noise (also known as white noise, thermal noise or Nyquist noise), generated by a resistor, depends on the temperature and the bandwidth. Shot noise generated by the quantized nature of charge is proportional to the bias current and the bandwidth. Noise generated in electronics is $1/f$ noise (also called flicker noise) which follows 1/frequency curve. The origin of the $1/f$ is not well-known. It may be explained by slow variations of the resistance given slow voltage fluctuations under constant current, by charging and discharging of an impurity (jumping of the conductance between more stable values), by technological processes ($1/f$ noise is more likely to appear close to metal-insulator transition), and so on [31]. Very often noise can be decreased by averaging over many measurements. Unfortunately, $1/f$ noise cannot be improved by averaging, it is a so-called “random walk” [31].

Typical working frequencies were 17.77 and 13.33 Hz. S4c current/voltage and S3b voltage/current source modules (of the IVVI-DAC rack) were employed to amplify the excitation signal, while measurement modules M2d voltage-measure and M1b current-measure were used to detect the signal. Model M2d has $0.8 \text{nV/} \sqrt{\text{Hz}}$ input noise voltage and model M1b has a noise floor down to $5 \text{ fA/} \sqrt{\text{Hz}}$.

### Table 1.1.
Calculated maximum applied voltage $V$ across the AB interferometer and maximum allowed current $I$ along the device for a quantum resistance $R_0 = h/e^2 = 26 \text{ kΩ}$ and for $R_{\text{max}} = 2 \text{ MΩ}$ at different temperatures $T$.

<table>
<thead>
<tr>
<th>$T$</th>
<th>$V$</th>
<th>$I(R_0)$</th>
<th>$I(R_{\text{max}})$</th>
</tr>
</thead>
<tbody>
<tr>
<td>10 mK</td>
<td>$k_BT$</td>
<td>0.86 µV</td>
<td>33.3 pA</td>
</tr>
<tr>
<td>3.5k_BT</td>
<td>3.01 µV</td>
<td>116.5 pA</td>
<td>1.51 pA</td>
</tr>
<tr>
<td>50 mK</td>
<td>$k_BT$</td>
<td>4.3 µV</td>
<td>166.5 pA</td>
</tr>
<tr>
<td>3.5k_BT</td>
<td>15.1 µV</td>
<td>0.58 nA</td>
<td>7.53 pA</td>
</tr>
<tr>
<td>100 mK</td>
<td>$k_BT$</td>
<td>8.6 µV</td>
<td>0.33 nA</td>
</tr>
<tr>
<td>3.5k_BT</td>
<td>30.1 µV</td>
<td>1.17 nA</td>
<td>15.1 pA</td>
</tr>
<tr>
<td>300 mK</td>
<td>$k_BT$</td>
<td>25.8 µV</td>
<td>0.99 nA</td>
</tr>
<tr>
<td>3.5k_BT</td>
<td>90.1 µV</td>
<td>3.49 nA</td>
<td>45.15 pA</td>
</tr>
<tr>
<td>500 mK</td>
<td>$k_BT$</td>
<td>43 µV</td>
<td>1.67 nA</td>
</tr>
<tr>
<td>3.5k_BT</td>
<td>150 µV</td>
<td>5.8 nA</td>
<td>75.3 pA</td>
</tr>
<tr>
<td>1 K</td>
<td>$k_BT$</td>
<td>86 µV</td>
<td>3.3 nA</td>
</tr>
<tr>
<td>3.5k_BT</td>
<td>301 µV</td>
<td>11.7 nA</td>
<td>151 pA</td>
</tr>
</tbody>
</table>
Apart from the noise, the interference is another kind of the disturbance in the measurement setup. To prevent interference in the system a few actions have to be taken: to prevent 50 Hz interference all elements directly connected to the sample are purely analog (no clock generator) and battery driven; the measurement setup consists of multiple twisted pairs in loops; all measurement elements were connected to a single ground and isolated from other possible ground connections by using wooden shelves for the measurement electronics, rubber pumping lines and plastic connectors for the helium recovery lines.

REFERENCES

Chapter 1


Chapter 2 Nanoparticle-Bridged Molecular Junctions

A high yield, reproducible and simple technique for fabrication of nanometer spaced electrodes by dielectrophoresis (DEP) is reported in this chapter. The method was used for the creation of molecular junctions by bridging a nanogap between gold leads, functionalized by a self-assembled organic monolayer (SAM), with gold nanoparticles (Au NPs) in order to study charge transport through self-assembled organic molecular monolayers. We perform electrical characterisation of the fabricated devices to examine transport properties dependent on the molecule’s characteristic (e.g. length, chemical composition, chemical bonding) and external parameters (e.g. temperature, electrostatic potential). We show an application of DEP method for fabrication of single-electron transistors (SETs) and designless Boolean logic devices.
Research interest in hybrid inorganic-organic electronics is increased in recent years. To be able to build molecule-based devices it is very important to study, understand and control electronic transport at the level of a single or a few molecular junctions. For this purpose building nanometer spaced gaps is necessary to embed single or a few molecules (with a common length in the order of 1-2 nm) in between. Standard top-down lithography technologies do not allow this. There are a few well-known techniques for the creation a single molecule device, such as mechanical break junctions [1], nanopores [2, 3], electromigration [4], shadow evaporation [5], scanning tunnelling microscopy [6]. Unfortunately, they are not very reproducible and require high skills and precision.

In this thesis a simple and very reproducible technique was chosen for the manipulation of single NPs and fabrication of molecular junctions and study charge transport properties of the molecular monolayers. This is the DEP manipulation method, which avoids the requirement for creating extremely small nanogaps (<1-2 nm) for the direct fabrication of a molecular bridge, and will be described below.

2.1. Dielectrophoresis Manipulation Method

DEP is a powerful tool for the controlled manipulation of small polarizable objects (such as metal and semiconducting particles, nanowires, DNA molecules and graphene) by a non-uniform electric field (Fig. 2.1) [7, 8]. This technique, introduced by Pohl [9], is widely used as a method for the creation of molecular junctions by bridging the nanogap between electrodes with NPs with great selectivity. When the electrodes are immersed into a liquid solvent, upon applying electric field the dissolved particles move towards the gap, where the electric field gradient is the largest (Fig. 2.1).

![Figure 2.1. Schematic picture of the DEP process.](image)
The DEP force acting on the particle strongly depends on the permittivities and the conductivities of the medium and the particle, particle’s volume and shape, time of the process, applied voltage and frequency. For a spherical particle the DEP force can be expressed as [8]:

\[ F_{\text{DEP}} = 2\pi\varepsilon_0\varepsilon_m a^3 \text{Re}[K(\omega)] \nabla E_{\text{rms}}^2 \]  

(2.1)

\[ \text{Re}[K(\omega)] = \frac{(\varepsilon_p - \varepsilon_m)(\varepsilon_p + 2\varepsilon_m) + \frac{1}{\omega^2}(\sigma_p - \sigma_m)(\sigma_p + 2\sigma_m)}{(\varepsilon_p + 2\varepsilon_m)^2 + \frac{1}{\omega^2}(\sigma_p + 2\sigma_m)^2}, \]  

(2.2)

where \( \varepsilon_m \) and \( \varepsilon_p \) are the permittivities of the medium and the particle, \( a \) is the radius of the NPs, \( K(\omega) \) is the Clausius-Mossotti factor, \( E_{\text{rms}} \) is the root-mean-square value of the electric field, \( \sigma_m \) and \( \sigma_p \) are the conductivities of the medium and the particle, and \( \omega \) is \( 2\pi f \).

### 2.2. Device Fabrication and Experimental Setup

Following the fabrication of the nanogaps and formation of the SAM on top of the electrodes, manipulation of the Au NPs and room temperature characterisation is carried out in a low temperature probe station. A sample is placed in the probe station and a colloidal solution of Au NPs is drop-casted on the sample’s surface. Afterwards AC (alternating) or DC (direct) voltage is applied across probe needles placed on top of the electrodes. A series resistor is tuned to prevent high current flow that could break the nanoscopic metallic electrodes, schematic image of the setup is depicted in Fig. 2.2.

![Figure 2.2. Schematic of the setup for the DEP trapping experiment. Cross-section of a nanogap, functionalized by the SAM and bridged with Au NP forming a metal-molecule-metal-molecule-metal contact.](image)

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The Clausius-Mossotti factor (Eq. 2.2) highly depends on the frequency of the applied voltage causing positive or negative DEP [10]. In this work AC voltage (generated by Stanford DS345 Function Generator) is set at 1 MHz and the amplitude of the signal is controlled by a custom-made LabView-based program. By varying Au NPs size (compare to the dimensions of the nanogap) and concentration in a solution, trapping time and voltage, it is possible to limit the amount of particles trapped between electrodes.

![Figure 2.3](image1.png)

**Figure 2.3.** Dependence of the DEP process on the NPs’ concentration. SEM images of 60 nm Au NPs trapped in a 50 nm nanogap (depicted in a) for different concentrations of NPs: b, original solution; c, 1:4 diluted in water; d, 1:10 diluted in water. Trapping time is 10 sec, AC voltage is 1 Vpp at 1 MHz, series resistance is 10 MΩ.

### 2.3. Concentration, Time and Voltage Dependences

In order to control the DEP procedure, trapping parameters have to be carefully adjusted. Two of the most important of them are the size and the concentration of the NPs in a medium. In this chapter commercially available citrate-functionalized 20, 60 and 100 nm in diameter Au NPs (British Biocell International) diluted in water with concentrations of $7.00 \times 10^{11}$, $2.60 \times 10^{10}$ and $5.60 \times 10^{9}$ particles/ml, respectively, are tested in all the experiments. As
shown in Fig. 2.3b, when the original solution of 60 nm Au NPs is used a NPs’ cluster forms around the 50 nm nanogap (Fig. 2.3a). Manipulation of one or a few NPs is possible after dilution of one part of the commercial solution with ten parts of the Milli-Q water (Fig. 2.3d).

When the NPs’ concentration is adjusted, Au nanorings (such geometry was used for the fabrication of hybrid inorganic-organic Aharonov-Bohm (AB) interferometers, see chapter 7) containing two nanogaps in parallel are used to test the trapping time and applied voltage. Figure 2.4 shows that both long trapping time and high peak-to-peak voltage lead to a formation of NPs’ cluster around nanogaps and appearing of the electromigration in the narrow interconnecting lines between the ring and contacting leads, causing formation of new nanogaps that are filled by NPs. A series resistor is introduced and tuned to 1 MΩ to limit the maximum current allowed in the system.

The analysis of all the devices shows that manipulation of an exact amount of NPs is very difficult. Nevertheless, controlling the trapping parameters allows to trap a number of NPs with a certain order of magnitude. In figures 2.5-2.6 there are examples of one and double parallel 50 nm nanogaps bridged by a single 60 nm Au NPs.

Figure 2.4. AFM images of 60 nm Au NP trapped in and around 40 nm nanogap embedded in the arms of Au AB ring. a-c, applied voltage is 1.5 V at 1 MHz, series resistance is 1 MΩ, trapping time is (a) 5 sec, (b) 10 sec and (c) 15 sec. d-f, trapping time is 5 sec, series resistance is 1 MΩ, applied voltage is (d) 1.7 V, (e) 1.9 V and (f) 2.2 V at 1 MHz.
Figure 2.5. SEM image of a single 60 nm Au NP trapped in a 40 nm nanogap. Trapping time is 5 sec, applied voltage 1.5 V at 1 MHz, series resistance is 1 MΩ.

Figure 2.6. AFM image of single 60 nm Au NP trapped in each 40 nm nanogap embedded in the arms of Au AB ring. Trapping time is 5 sec, applied voltage 1.7 V at 1 MHz, series resistance is 1 MΩ.

2.4. Current-Voltage Measurements through Molecular Monolayers in Nanoparticle Bridges

Preliminary characterisation of the charge transport through molecular SAMs in NPs bridges is performed in vacuum (below $10^{-4}$ mbar) and at room temperature. Current-voltage ($I$-$V$) measurements are carried out in a probe station in a two-probe configuration using a Keithley 2400 SourceMeter and
controlled via a custom-made LabView-based program. Figure 2.7 shows a representative $I$-$V$ characteristic for one of the devices (100 nm Au NP bridge junction coated by 1,5-pentanethiol). The non-linear behaviour in Fig. 2.7 is typical of coherent non-resonant charge tunnelling, which has been widely observed for charge transport through molecular junctions [11-13] (Section 1.4).

Devices showing such non-linear behaviour are taken into account as “working”. When a short is measured or the signal is in the noise level, the devices are considered as “non-working” and their data is excluded from this thesis. The yield of the “working devices” is about 50%.

![Figure 2.7. $I$-$V$ characteristic of a junction coated by 1,5-pentanethiol and bridged by 100 nm Au NP showing the non-resonant tunnelling behaviour. $T=295$ K.](image)

The examination of characteristic temperature, length, structure and contact dependences on the charge transport is necessary for the reason that it can reveal the charge transport mechanism through molecular SAMs. Figure 2.8 shows statistical histograms of $\log_{10}[R(\Omega)]$ (R is the resistance of the junction), measured at 0.1 V for the junctions bridged by 60 nm Au NPs and functionalized by 1,5-pentanethiol (Fig. 2.8, green), 1,6-hexanethiol (Fig. 2.8, red) and 1,9-nonanethiol (Fig. 2.8, blue), representing the length
dependence through the dithiol molecules. Such a statistical analysis based on a large amount of measurements data is of high importance due to the reliability issues of molecular junctions [7, 13, 14].

**Figure 2.8.** Statistical histograms of $\log_{10}[R(\Omega)]$ measured at 0.1 V for 40 nm Au junctions bridged by 60 nm Au NPs and functionalized by 1,5-pentanediethiol (green), 1,6-hexanediethiol (red) and 1,9-nonanediethiol (blue).

**Figure 2.9.** Semilog plot of $\log_{10}[R(\Omega)]$ versus the chain length of the alkanediethiols. The extracted decay factor is $1.1\pm0.1$ Å⁻¹.
Transport through alkanedithiols is in general a coherent tunnelling which strongly depends on the effective contact resistance and the tunnelling decay factor $\beta$ (Eq. 1.8) (Section 1.4). The semilog plot in fig. 2.9 represents a clear exponential dependence of the resistance on the length of the alkanedithiol chain, based on the data represented in fig. 2.8. The decay factor extracted from the linear fit is $1.1\pm0.1$ Å$^{-1}$ and in good agreement with the literature values which lie between 0.75 and 1.15 Å$^{-1}$ [13, 15]. Thuo and Reus, et al [14] demonstrated a difference in rates of charge transport through molecular SAMs with odd- and even-numbered $n$-alkanediethiols. This fact may explain the lowered position of the data point for 1, 6-hexanediethiol with respect to the linear fit in fig. 2.9.

Electrical measurements at different temperatures show, in accordance with the theory and literature, that the electron transport through alkanediethiols weakly depends on the external parameters such a temperature and magnetic field. (Measurement data is not included in this thesis). The influence of the anchoring group is not studied in present work.

Figure 2.10 represents statistical histograms of $\log_{10}[R(\Omega)]$ measured at 0.1 V for the junctions bridged by 60 nm Au NPs and functionalized by 4,4’-dimercaptostilbene (OPV2) and S,S’-[1,4-Phenylenebis(2,1-ethynediyl-4,1-phenylene)]bis(thioacetate) (OPE3), and based on the data from “working” devices. As expected [16, 17], OPV2 and OPE3 are better conductors than alkanes, and OPV2 molecules show much lower resistance compare to OPE3.

![Figure 2.10. Statistical histograms of $\log_{10}[R(\Omega)]$ measured at 0.1 V for 40 nm Au junctions bridged by 60 nm Au NPs and functionalized by 4,4’-dimercaptostilbene (red) and S,S’-[1,4-Phenylenebis(2,1-ethynediyl-4,1-phenylene)]bis(thioacetate) (blue).]
2.5. Molecular Exchange

An additional advantage of the DEP is that molecular exchange can be performed without changing the device structure. Molecular exchange is a chemical process able to replace the molecules of a SAM monolayer by simply immersing the device in a different molecular solution. If the concentration of the new molecules and the strength of the new chemical bonds is high enough, the new molecules will replace the old ones forming a new SAM. Bernard et al. [18] demonstrated successful molecular exchange between the conjugated oligomers and alkanethiol SAMs with a NPs array network. Molecular exchange in a 60 nm Au NPs bridged molecular junction is depicted in Fig. 2.11. Observed change in the resistance with every exchange step is in agreement with the previously obtained results (Section 1.4).

![Figure 2.11. a, AFM image of the ring containing 40 nm junctions and bridges by 60 nm in diameter Au NPs. b, Dependence of the resistance through the metal-molecule-NPs-molecule-metal parallel junctions (depicted in a) on the molecule for different exchange steps: (1) 4,4'-Bis(mercaptomethyl)biphenyl; (2) 1,9-Nonanedithiol; (3) 1,6-Hexanedithiol; (4) 1,4-Benzenedimethanethiol; (5) 4,4'-Dimercaptostilbene; (6) 1,9-Nonanedithiol; (7) after O$_2$ ashing; (7) after the cleaning with HNO$_3$.](image)

More detailed analysis is performed for the molecular exchange of OPE3 by OPV2 molecules in Au NPs bridged junctions (Fig. 2.12), which shows that for the average of more than 10 samples the tendency of the decreasing resistance remains the same [16].
Nanoparticle-Bridged Molecular Junctions

Figure 2.12. Statistical histograms of $\log_{10}[R(\Omega)]$ measured at 0.1 V for 40 nm Au junctions bridged by 60 nm Au NPs and functionalized by S,S'-[1,4-Phenylenebis(2,1-ethylenediyl-4,1-phenylene)]bis(thioacetate) (blue) and later exchanged by 4,4'-dimercaptostilbene (red).

2.6. Single-Electron Transistor

Low temperature measurements reveal another advantage of the DEP. NPs trapping between electrodes functionalized by molecular SAMs allows us to create a SET where SAMs play a role as tunnel barriers between electrodes and NPs. Charge transport measurements at a temperature of 22 mK show a clear Coulomb blockade and Coulomb diamonds, demonstrating that the transport is from two or more NPs (see chapter 5).

An Au AB ring containing 40 nm gap between the ring and the interconnecting leads was functionalized by 1,6-hexanedithiol and 60 nm Au NPs were trapped in the gap. Figure 2.13 represents the differential conductance ($dI/dV$) as a function of source-drain voltage ($V_{SD}$) and back-gate voltage ($V_G$) at a temperature of 22 mK (as a back gate p++Si is used underneath 35 nm of SiO$_2$). The measurements were performed in a cryogen-free dilution refrigerator in a two point configuration using a low-noise technique (Section 1.8). Charging energy of the SET is about $E_C=0.7$ meV.

The advantage of the SET fabrication via DEP is that the charging energy of the device can be tuned by careful choice of the molecular SAM and the type and size of the NPs. Using molecular exchange, simply by dipping the device in a fresh solution with new molecules, the charging energy can be significantly changed without building up a new device (Chapter 4).
Furthermore, by choosing smaller NPs or semiconductor NPs, it is possible to reveal more fundamental physical effects [19].

Figure 2.13. a, AFM image of the Au ring containing a gap on the side bridged by 60 nm Au NPs. b, Differential conductance (dI/dV) of the device in a as a function of the source-drain voltage (V_{SD}) and back gate voltage (V_{G}) at a temperature of 22 mK (B=8 T).

2.7. Evolution of the Designless Nanoparticle Network into Boolean Logic

By increasing trapping time and NPs concentration in a solution during DEP procedure it is possible to create an isolated designless NPs network. Figure 2.14b shows an example of such disordered network of 20 nm Au NPs trapped in a circular region (200 nm in diameter) between twelve metal electrodes (Fig. 2.14a). For such electrode configuration NPs trapping is performed sequentially with pairs of diametrically opposite electrodes, by contacting the pads with the probe-station needles.

Based on the idea of the fabrication of disordered NPs network via NPs trapping Bose, Lawrence et al. [20] experimentally shown that below the temperature of 5 K, when each particle isolated by 1-octanethiol acts as a SET, a network of randomly assembled Au NPs can be configured in situ into any of the commonly used 2-input Boolean logic gates by a small set of control voltages.
Figure 2.14. NP network. a, SEM image of 12 Au electrodes with an inner spacing of 200 nm. b, AFM image of 20 nm Au NPs trapped between electrodes depicted in a.

Conclusions

DEP is a high yield, simple and reproducible processing technique for combining top-down and bottom-up fabrication approaches. It is a quick and easy method which allows electrical characterisation of a large number of molecules and exchanging molecules in the junction. Electrical measurements shown that the electron transport weakly depends on the external parameters such as temperature and magnetic field. On the other hand, molecule's characteristics (such as length and chemical composition) play an important role in the transport. An increase of the molecule length causes an exponential decrease in the molecule’s conductance. By varying the chemical composition it is possible to change the resistance through the molecular junction from GigaOhms for long non-conjugated molecules to kiloOhms for short or conjugated ones. Performed experiments show that molecules in the molecular junction can be exchanged without fabrication of a new device. The Coulomb blockade regime can be achieved at cryogenic temperatures in a metal-molecule-NP-molecule-metal junction created via DEP. The obtained results show that the used DEP technique is an effective and easy method for studying different molecular layers and can be used for investigating charge transport through the molecular junctions.
REFERENCES


Nanoparticle-Bridged Molecular Junctions


Chapter 3 Wedging Transfer Technique

This chapter is dedicated to the experimental investigation of the wedging transfer technique and implementation of the method for soft landing of an electrical contact on top of the bottom electrode functionalized by a self-assembled monolayer (SAM) in order to create nanoscopic molecular junctions for the investigation of the charge transport through organic monolayers. Electrical characterisation was employed to test charge transport dependence on the temperature and molecule’s length. We also compare properties of molecular junctions made via wedging transfer technique and dielectrophoresis (DEP) manipulation method.
Chapter 3

The biggest challenge for studying charge transport through molecular layers is the creation of molecular junctions. In chapter 2 we have discussed the investigation of molecular junctions fabricated via DEP manipulation method. Particularly, the nanoparticles (NPs) trapping technique was tested. In this chapter we explore wedging transfer as an alternative method for the fabrication of nanoscopic molecular junctions. Via this technique a top electrical contact can be soft-landed on top of the bottom electrode functionalized by SAM avoiding direct metal evaporation which can lead to metal filaments piercing through the monolayer causing shorts [1, 2].

3.1. Wedging Transfer as an Alternative Method for the Creation of Molecular Junctions

Wedging transfer is a relatively new technique for transferring nano- and microstructures of various shapes and compositions onto different types of surfaces [3-5]. In the basis of the method lies the hydrophilic/hydrophobic effect: water “likes” to wet hydrophilic surfaces and avoid hydrophobic ones. When a hydrophilic substrate containing a hydrophilic object is immersed in water, water lifts-off the object from the substrate.

In 2013, Krabbenborg, Wilbers et al. applied wedging transfer for the first time for fabrication and electrical characterisation of the large-area (100-400 µm²) metal-molecular monolayer-metal junctions [4]. In this thesis the method is adopted for the creation of molecular junctions at nanoscale. The schematic of the wedging transfer is depicted in fig. 3.1. The process consist of the following steps:

- a hydrophilic substrate containing a hydrophobic object is treated by ozone to increase hydrophilicity of the surface;
- a hydrophobic polymer is dip coated on the top of the sample and let dry;
- substrate is immersed in water where polymer is lifted-off pilling off the object;
- floating on water surface polymer containing the object is aligned to a preliminary cleaned nanogap and functionalized by the SAM while water is slowly pumped out;
- bringing together the object covered by a polymer and the SAM-covered nanogap;
- dissolving the polymer.
**Figure 3.1.** Schematic of the wedging transfer process.
Chapter 3

3.2. Device Fabrication

To increase the yield of well-aligned devices, the design of the nanogaps and dots “to-be-transferred” has to be chosen carefully due to the difficulty of the alignment procedure (see below) of the floating polymer to the substrate containing nanogaps. If the distance between dots is \( s \), then the first two nanogaps should be shifted in \( y \)-direction by \( s/2 \) relatively to each other, while the second two nanogaps should be shifted by \( s/2 \) in \( x \)-direction relatively to the first two gaps (Fig. 3.2).

![Diagram of nanogap design](image)

**Figure 3.2.** Schematic of the possible design of the junctions and transferred dots (depicted as circles).

A group of four gaps is repeated 60 times in a matrix of 5×12 groups on one 11×11 mm² Si/SiO₂ substrate. Nanodots (<\( s \) in diameter, spaced by the distance \( s \)) are patterned in sixty 150×150 µm² square areas repeating the design of nanogaps. Ideally, during the alignment procedure one out of four gaps should be “hit” by an island. The amount of built dots is limited by electron beam lithography writing time.

Atomic force microscopy images showing experimental results of the wedging transfer fabrication process are depicted in fig. 3.3. Here, 200×200 nm² Au dots (Fig. 3.3b) are transferred on top of 40 nm Au gaps functionalized by a SAM (Fig. 3.3a), resulting in the creation of metal-molecular monolayer-metal nanojunctions (Fig. 3.3c). As can been seen in the fig. 3.3c, one 40 nm Au gap is covered by 200×200 nm² Au island.
Figure 3.3. AFM images showing the wedging transfer fabrication process. a, 40 nm Au nanogaps; b, 200 nm square Au dots “to be transferred” on top of the nanogaps in a; c, Au dots in b transferred on top of Au nanogaps in a (high-lighted by blue circle).

Figure 3.4. Optical image of the 200 nm square Au dots attached to the cellulose floating in water above a Si/SiO₂ substrate, containing 40 nm Au nanogaps covered by self-assembled monolayer.
Chapter 3

The optical image in Fig. 3.4 shows the alignment procedure of the floating-on-water-polymer with 150×150 µm² square areas containing Au 200×200 nm² square islands on top of groups of four 40 nm Au gaps connected to the 100×100 µm² contacting pads (used to connect probes for the electrical characterisation). Due to the micrometer-sized features a microscope lens with a short focal distance has to be used. That leads to difficulties for the use of the manipulation probe needles and water-pumping syringes. As a result the alignment has to be performed by hand what can influence the quality and the yield of the working devices.

3.3. Molecular Length Dependence

Immediately after the device fabrication (to prevent degradation of the molecular SAM) electrical characterisation of nanojunctions is performed in vacuum (<10⁻⁴ mbar) first at room and then low (5 K) temperatures. Current-voltage (I-V) measurements are carried out in a probe station in a two-probe configuration using Keithley 2400 SourceMeter and controlled via custom-made LabView-based program.

In this thesis for the examination of the molecular length dependence, molecular junctions containing alkanethiol SAMs with six, eight and ten carbons are fabricated and electrically characterised. Only devices showing non-linear Simmons behaviour [6-8] are considered as “working” (Table 3.1) and are represented in statistical histograms of \( \log_{10}[R(\Omega)] \) (\( R \) is the resistance of the device) (Figs. 3.5-3.6). Based on the measured resistance, the devices are divided into “non-working” (when a short is measured or the signal is in the noise level) and “working”. The data of the “non-working” devices is excluded from this thesis. The yield of the “working” devices is varying for different molecules. Due to the extremely small (~ 5%) yield of the “working” devices for the 1,10-decanedithiol, statistical analysis of the experimental data cannot be performed and is excluded from this thesis.

<table>
<thead>
<tr>
<th>( N_C )</th>
<th>Total number of junctions</th>
<th>Yield, %</th>
</tr>
</thead>
<tbody>
<tr>
<td>6</td>
<td>60</td>
<td>45</td>
</tr>
<tr>
<td>8</td>
<td>120</td>
<td>23</td>
</tr>
<tr>
<td>10</td>
<td>120</td>
<td>5</td>
</tr>
</tbody>
</table>

Table 3.1. Working device yield for measurements of molecular junctions with alkanethiol SAMs of different length (\( N_C \)).

Figures 3.5-3.6 represent statistical histograms of \( \log_{10}[R(\Omega)] \) measured at 0.1 V for the junctions created via the wedging transfer technique and functionalized by 1,6-hexanethiol and 1,8-octanethiol, and based on the data from “working” devices. Unfortunately, due to the lack of data for
1,10-decanedithiol, the length dependence cannot be plotted. Yet, comparison of the data in Figs. 3.5-3.6 to the semilog plot in Fig. 2.9 shows that molecular SAMs junctions created via wedging transfer technique are more conducting than junctions fabricated by means of NP bridge, as we will further discuss in the next section.

Figure 3.5. Statistical histograms of $\log_{10}[R(\Omega)]$ measured at 0.1 V for the 40 nm Au junctions functionalized by 1,6-hexanethiol and bridged by 200x200 $\mu$m$^2$ square Au dots.

Figure 3.6. Statistical histograms of $\log_{10}[R(\Omega)]$ measured at 0.1 V for the 40 nm Au junctions functionalized by 1,10-octanethiol and bridged by 200 x200 $\mu$m$^2$ square Au dots.
3.4. **Comparison of the Molecular Junctions Made via Nanoparticle Bridge to the Molecular Junctions Created via Wedging Transfer Technique**

Relying on the data obtained from the electrical measurements on the molecular junctions created via NP bridging (Chapter 2) and wedging transfer a comparison between two techniques can be performed. Schematics of the molecular junctions created by means of a NP bridge and wedging transfer are depicted in Fig. 3.7.

As it was discussed in chapter 1 non-resonant tunnelling charge transport through molecular SAMs is proportional to the effective contact resistance $R_0$ (Eq. 1.10) which depends on the anchoring group and the contact electrodes. In the case of alkanedithiols the sulfhydryl (–SH) group is used as an anchoring group to attach the alkane chain to gold. Nevertheless, the interface between SAMs and electrodes plays a crucial role influencing the coupling of the anchoring group to the metal.

![Figure 3.7](image)

**Figure 3.7.** Schematics of the molecular junctions created via wedging transfer (a-b) and via nanoparticle bridge (c-d). Cit$^-$ represents citrate molecules.

Prior to the wedging transfer the top electrode is electron-beam evaporated on top of thermally grown SiO$_2$, what leads to the formation of a very flat bottom surface of the top electrode [4] which is later landed on top of
the molecular SAM during wedging transfer procedure (Fig. 3.7a,b). However, most of commercially Au NPs are covered by citrate layer which is stabilizing the particles in solution. Thereby, when NP is placed on top of the molecular SAM there is a citrate layer between the SAM and the NP which can lead to bad coupling of the molecules to the metal (Figs. 3.7c,d). This might explain lower resistance measured in devices made via wedging transfer compared to the NPs bridges (Figs. 2.8, 3.5-3.6). Another reason could be that the cross-section area of the molecular junction created via wedging transfer is bigger than the area of NP bridged junctions.

Another characteristic differing NP bridging from wedging transfer technique is a possibility to build a single-electron transistor. The charging energy is inversely proportional to the capacitance of an object which scales with its radius [9]. Commercially available NPs are not bigger than 120 nm in diameter while the size of the nanoisland, fabricated via the wedging transfer technique, is unlimited and determined by experimentalist’s design.

Conclusions

Wedging transfer is a promising technique for the fabrication and electrical characterisation of nanoscopic molecular junctions. Electrical characterisation demonstrated that the junctions created via wedging transfer are more conductive than junctions fabricated via NPs bridging. The yield of the working devices was shown to be lower than 50% which could be improved, for example, by the immersing of the bottom electrode into SiO₂ to flatten the edges or by using metal with a smoother surface. Due to the expected low charging energies of the transferred metallic islands, wedging transfer has an advantage when low temperature measurements on molecular layer have to be done.

REFERENCES


In this chapter*, we report a new reproducible technique for the fabrication of single-electron transistors (SETs) based on Au nanoparticles (NPs). We combine top-down lithography and bottom-up self-assembly of Au NPs and Au nanorods (NRs), bridging the gap between the nano- and microscale. By means of selective chemical interactions, functionalised Au NRs and Au NPs in dispersion self-assemble into NR-NP-NR assemblies. The NR-NP-NR assemblies are deposited on a highly doped Si/SiO₂ substrate and electrically contacted with metal electrodes defined by electron beam lithography (EBL) obtaining SETs with the substrate acting as a back gate. After the device fabrication, we replace the linker molecules (homocysteine) between the NPs and NRs with 1,8-octanedithiol. The molecular barrier decouples single NP from the two NR-contacts, as demonstrated by the clear Coulomb blockade features observed at low-temperature (<15K) in the charge-transport measurements.

* K.S. Makarenko†, Z. Liu† et al, in preparation
4.1. Self-Assembly of a Single Nanoparticle to two Gold Nanorods

Over the last few decades semiconductor electronics has evolved extremely successfully, based on the miniaturization of silicon transistors. This ongoing miniaturization is largely enabled by the developments in top-down fabrication methods. However, as we are approaching critical features of \(~10\) nm, top-down fabrication becomes so challenging and costly that alternative fabrication schemes are most probably required. According to the International Technological Roadmap for Semiconductors (ITRS) electronic circuits will already reach this limit within a decade [1].

Connecting single nanostructures and molecules to electric circuitry has proven to be an extremely difficult task. Many (top-down) schemes have been developed [2-8]. These techniques, however, often suffer from serious intrinsic problems, such as poor reproducibility, lack of control of number and orientation of nanostructures and damage due to fabrication. The synthesis of inorganic materials with dimensions on the nanometer scale has greatly improved in recent years [9, 10]. For example, hierarchical integration of nanoscale building blocks (nanoparticles, nanorods, nanotubes etc.) into functional assemblies, and further into functional devices is suggested to be achieved through a “bottom-up approach” [11-13]. Examples include dimer gold nanoparticles linked by organic dithiol molecules [11], the preparation of ordered metal-molecule-metal networks by photosensitive molecules [12], and photolithography linkage of ZnO nanowires [13]. Au NRs have gained much attention due to their wide range of applications as “interconnectors” in nanoscale devices [14]. End-to-end self-assembly of Au NRs has previously been reported through electrostatic interactions [15, 16], H-bonding/covalent bonding [17], and avidin-biotin interactions [18]. Similarly, one-dimensional self-assembly of Au NPs has also been reported driven by diverse chemical interactions [19-21].

Those initial one-component systems (component referring to the type of nanostructure involved) have already increased our understanding of particle-particle interactions on the nanometer scale, and also formed an inspiration for the development of our new way to prepare multi-component assemblies for the realization of nanoelectronic devices.

We proposed an unconventional way of realizing functional nanoelectronic devices (in particular SETs) using a chemical (bottom-up fabrication) approach based on self-assembly and chemical recognition (Fig. 4.1). We combine self-assembly and molecular recognition at nanoscale on one side with conventional top-down technology at larger scale on the other side which forms an innovative path to bridge the micro-nanogap.
Compared to previous methods, our strategy has several advantages. First, a single Au NP is linked to two NRs of ~250 nm length, making the total size of the assembly large enough to connect it relatively easily to electrodes using standard EBL. Second, the chemical linkage between the Au NP and the Au NRs is well-defined and tunable by chemical engineering. Third, there is great flexibility in choosing the nano objects to be electrically connected: a metallic nanoparticle, a semiconductor quantum dot or a single molecule. Last but not least, bottom-up assembly has in principle the potential to produce vast amounts of the desired assembly in parallel. Moreover, our approach is interesting from a chemistry point of view, in particular the control/guidance and limitation of self-assembly and complexity.

To the best of our knowledge, our specific approach – chemically connecting Au NPs to Au NRs – have never been used for the purpose of bottom-up fabricated nanoelectronic devices.

Figure 4.1. Schematic representation of the bottom-up self-assembly combined with top-down lithography to realize a SET based on a single Au NP. a-b, Formation of the NR-NP-NR assembly by means of selective chemical interactions and deposition of the assembly on a substrate; c, contacting of the assembly with metal electrodes defined by EBL.
4.2. Sample Fabrication

4.2.1. Bottom-Up Approach*

Studies of the Au NR crystal structure show that the end facets of Au NRs are dominated by (111) planes, and the side facets by (110) and (100) planes [22-24]. Thiol groups preferentially bind to the (111) planes [17, 18] at low concentration. Based on this selective modification of the Au NRs ends, the specific chemical interactions are expected with preferably the ends of the Au NRs. We propose that Au NRs might link with a single Au NP due to the selective chemical interactions. We tested a few methods (e.g., click-chemistry, “host”-“guest” interactions) to form the assemblies. Nevertheless, the highest yield was achieved with a homocysteine, a thiol-containing amino acid, as a linker molecule between Au NRs and Au NP. At pH 6.5, around the isoelectric point of homocysteine, it becomes zwitterionic. The zwitterionic groups at the Au NRs ends and the NP cause attraction through a two-point electrostatic attraction in a cooperative fashion (Fig. 4.1). The NP needs to react with thiols, so Au NPs were chosen.

Cetyltrimethylammonium bromide (CTAB) stabilized Au NPs were prepared by adding 200 μL citrate stabilized Au NPs into 800 μL CTAB aqueous solution (25 mM) under ultra-sonication. For the assembly of the Au NRs with NPs, 5 μL CTAB stabilized Au NPs were mixed with 200 μL Au NRs under shaking, then 2 μL fresh homocysteine aqueous solution (1 mM) were added into the colloidal solution. The dispersion was shaken and then kept at room temperature for 2 hours.

To prepare the sample for top-down lithography, the mixed dispersion was transferred onto a Si/SiO2 substrate with markers (Figs. 1.9, 4.2a) cleaned for 10 min with oxygen plasma. The sample was left for 20 minutes for NR-NP-NR to precipitate. Afterwards, the dispersion containing non-precipitated assemblies was blown away by high pressure nitrogen gas. Subsequently, the substrate was immersed in 5 mM 1,8-octanedithiol ethanol solution for 24 hours to ensure that all of the homocysteine molecules were exchanged by 1,8-octanediol (we believe that homocysteine might not survive the fabrication procedure). Prior to EBL, the substrate was taken out from the dithiol solution and washed by a large amount of ethanol and dried by nitrogen gas (Fig. 4.2a).

* The bottom-up approach was realized by Zhihua Liu
Figure 4.2. Bottom-up self-assembled SET. a, AFM image of the NR-NP-NR assemblies deposited on a Si/SiO₂ wafer containing pre-patterned bitmap markers (inside yellow squares). Inset shows an assembly chosen for contacting. b, SEM image of the device (inset in a) contacted with EBL.
4.2.2. Top-Down Approach

After the deposition of the NR-NP-NR assemblies, samples were imaged by AFM in order to find candidates for the EBL contacting. (In section 1.6.2 it was discussed why scanning electron microscopy (SEM) has to be avoided). Figure 4.2a shows a typical AFM image, where NR-NP-NR assemblies and bitmap markers (high-lighted by yellow squares) can be seen. The AFM images of selected candidates were used for the EBL design of the contacting electrodes. After the design preparation, samples were covered by 220 nm thick resist PMMA 950 A4. Our experiments have shown that prebaking of the resist resulted in a formation of short circuits between NRs and NPs. To avoid this, samples were left over night for the degassing of the resist solvent on a wet bench covered by a glass beaker and with a nitrogen flow access. Afterwards, an EBL was performed to define the contacts (Chapter 1).

In order to reach an EBL alignment accuracy better than 20 nm, we used alignment markers (Section 1.6.1). Just prior to the metal evaporation the samples were cleaned with an oxygen plasma (in order to remove resist residuals) and rinsed in ethanol (for the removal of gold oxide). Immediately after metal evaporation (40 nm of Au on top of 3 nm Ti) samples were dipped into 5 mM 1,8-octanedithiol acetone solution for a lift-off procedure. Following the lift-off, samples were bonded and electrically tested. Figure 4.2b shows an electrically contacted SET (one out of more than 15 devices) illustrated in the inset of Fig. 4.2a.

4.3. Electron Transport through Bottom-up Self-Assembled Single-Electron Transistors

4.3.1. Self-Assembled Single Electron Transistors of Different Sizes

Low-noise low-temperature measurements reveal a classical Coulomb blockade regime. Figure 4.3 shows a differential conductance \( \frac{dI}{dV} \) as a function of the source-drain voltage \( V_{\text{bias}} \) and back gate voltage \( V_{\text{gate}} \) at temperature <15 mK, showing the electron transport through SETs of different sizes. Around zero bias the conductance is suppressed and can be controlled by applying \( V_{\text{bias}} \) and \( V_{\text{gate}} \). The charging energy of a Coulomb island is inversely proportional to the size of the island [25]. Our experiments have shown this trend. From Figs. 4.3a,b it can be seen that the smaller particle gives much bigger charging energy (~25.8 meV for the 20 nm Au NP and 8.14 meV for the ~100 nm Au flake). Calculated coupling parameters are shown in Table 4.1.
Figure 4.3. Two-dimensional plots of differential conductance as a function of bias voltage $V_{\text{bias}}$ and gate voltage $V_{\text{gate}}$ through SETs fabricated by selective chemical interactions for two different sizes of Coulomb islands: (a) ~100 nm Au flake and (b) ~20 nm Au NP. Insets demonstrate AFM (a) and SEM (b) images of the corresponding devices. Blue areas inside inset in (a) show the design of the contacting electrodes prepared by electron beam lithography. ($T<15$ mK).
4.3.2. Temperature Dependence of the Electron Transport in a Single-Electron Transistor

Due to the size and nature of the studied Coulomb islands (~20 nm in diameter Au NPs) we assume, that the transport through the SETs is a typical classical, or metallic, Coulomb blockade [26, 27]. We studied the temperature dependence of the Coulomb oscillations of SETs. Figure 4.4 shows the temperature dependence of the full-width at the half-maximum (FWHM) of the Coulomb peak in Fig. 4.5 of the device in Fig. 4.6. Here, the top left inset shows the dependence at lower temperatures while the lower right inset shows the Coulomb peak at $T = 7$ mK (base temperature) fitted with Lorentzian function (tunnelling broadening $\hbar \Gamma$, in red, see Section 1.3) and Eq. 1.9 corresponding to the thermal broadening $k_B T$ in the classical regime (in blue) [28]. From this fitting we can conclude that the peak width is mainly determined by thermal broadening: $\hbar \Gamma \ll k_B T$. (extracted from the fitting corresponding energies are 0.06 µeV and 7.45 µeV, respectively).

The temperature of the electrons in the device (or effective electron temperature $T_e$) can differ from the temperature of the dilution refrigerator temperature $T$, mainly due to the noise and pick-up interference (Section 1.8). We can estimate the effective electron temperature from the plot in Fig. 4.4. The slope of the temperature dependence gives a thermal broadening of $4.3 k_B T$ (for the $\alpha$-factor equal to 0.095, extracted from the Coulomb diamonds in Fig. 4.6). This is in good agreement with the theory [28], where the FWHM

---

**Table 4.1.** Calculation of the coupling and interaction parameters of Coulomb islands shown in Fig. 4.3 (see Fig. 1.3 for details).

<table>
<thead>
<tr>
<th></th>
<th>100 nm Au flake</th>
<th>20 nm Au NP</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\Delta V_{\text{gate}}$</td>
<td>20 ± 0.3 mV</td>
<td>146 ± 2.0 mV</td>
</tr>
<tr>
<td>$k_1$</td>
<td>1.038</td>
<td>0.408</td>
</tr>
<tr>
<td>$k_2$</td>
<td>0.669</td>
<td>0.313</td>
</tr>
<tr>
<td>$\alpha_g = k_1 k_2 / k_1 + k_2$</td>
<td>0.407</td>
<td>0.177</td>
</tr>
<tr>
<td>$C_g = e / \Delta V_{\text{gate}}$</td>
<td>8.01 $\cdot 10^{-18}$ F</td>
<td>1.1 $\cdot 10^{-18}$ F</td>
</tr>
<tr>
<td>$C_s = C_g / k_1$</td>
<td>7.72 $\cdot 10^{-18}$ F</td>
<td>2.7 $\cdot 10^{-18}$ F</td>
</tr>
<tr>
<td>$C_d = C_g / k_2 - C_g$</td>
<td>3.96 $\cdot 10^{-18}$ F</td>
<td>2.4 $\cdot 10^{-18}$ F</td>
</tr>
<tr>
<td>$C = C_g + C_s + C_d$</td>
<td>1.97 $\cdot 10^{-17}$ F</td>
<td>6.2 $\cdot 10^{-18}$ F</td>
</tr>
<tr>
<td>$\Delta V_{\text{bias}} = \alpha_g \Delta V_{\text{gate}}$</td>
<td>8.14 ± 0.1 mV</td>
<td>25.8 ± 0.4 mV</td>
</tr>
</tbody>
</table>
of the Coulomb peak is predicted to be $4.35 k_B T$ for multilevel conductance and supported by experiments in [29]. The FWHM of the peak at 7 mK is equal to 7.45 μV. This gives us the effective electron temperature $T_e = 23 \pm 1$ mK.

Figure 4.7 shows a typical temperature dependence of the Coulomb oscillations of one of the devices (Fig. 4.3b). In line with theory [29] the Coulomb peak maximum is independent of the temperature as long as $4.3 k_B T \ll e^2 / C$ (~69.7±1.1 K, where $e^2 / C = 25.8 \pm 0.4$ meV extracted from Fig. 4.6) as predicted for metallic islands (Section 1.3).

**Figure 4.4.** Temperature dependence of the full width at half maximum of the Coulomb peak in Fig. 4.5 ($\alpha$-factor =0.095 is extracted from the Coulomb diamonds in Fig. 4.6). Top left inset shows the dependence at lower temperatures. Lower right inset shows Coulomb peak at $T=7$ mK fitted with Lorentzian function (tunnelling broadening, in red) and for a thermal broadening (Eq. 1.9, in blue).

**Figure 4.5.** Temperature dependence of the Coulomb peak of the single-electron transistor in Fig. 4.6 ($V_{\text{bias}}=5$ μV).
Figure 4.6. Differential conductance as a function of bias voltage $V_{\text{bias}}$ and gate voltage $V_{\text{gate}}$ of a SET fabricated by selective chemical interactions for a 20 nm Au NP ($T<15$ mK). Inset: SEM image of the corresponding SET.

Figure 4.7. Temperature dependence of the Coulomb oscillations of the SET in Fig. 4.3b ($V_{\text{bias}}=1$ mV).
4.4. Molecular Exchange

Exchange of the organic ligand molecules around the Au NPs can be performed without changing the structure of the devices (Section 2.5). Here, we show that molecular exchange can change the electronic properties of the SETs made by means of selective chemical interactions. In Figures 4.8-4.9 the electron transport measurements through two different devices is shown before and after replacing the 1,8-octanedithiol shell with S,S’-[1,4-Phenylenebis(2,1-ethynediyl-4,1-phenylene)]bis(thioacetate) (OPE3).

![Figure 4.8](image)

**Figure 4.8.** Differential conductance as a function of source-drain voltage $V_{\text{bias}}$ and gate voltage $V_{\text{gate}}$ of a SET fabricated by selective chemical interactions containing 20 nm Au NP ($T<15$ mK) before (a) and after (b) molecular exchange. Inset in (a) demonstrates SEM image of corresponding device.
Figure 4.9. Coulomb oscillations through the SET in the inset in Fig. 4.8a showing the increased conductance through the device after molecular exchange of 1,8-dithiol (red) with OPE3 (blue) ($V_{\text{bias}}=10 \, \mu\text{V}, T<15 \, \text{mK}$).

For the device in Fig. 4.8 the charging energy changes from 20.8 meV (Fig. 4.8a) to 18.4 meV (Fig. 4.8b) (extracted from the differential conductance plots), as well as the coupling to the source/drain obtained more asymmetrical character (what can be explained by the molecular exchange chemical processes which are not studied deeply in present work). Figure 4.9 shows Coulomb oscillations demonstrating that the conductance through the device increased after molecular exchange in agreement with literature. Another device (Fig. 4.10) shows besides decreased charging energy new features (Fig. 4.10b) which might be due to the vibrational modes. (No effect was observed in magnetoresistance measurements).

Conclusions

We have shown a novel reproducible (>50%) method for the fabrication of single-electron transistors via combination of bottom-up self-assembly of nano-objects and top-down lithography. Electrical characterisation at low temperatures revealed a classical Coulomb blockade regime. We investigated Coulomb islands’ size and temperature dependences on the SETs’ performance. By varying the nature and size of the Coulomb islands (as well as the type of molecular barrier) it is possible to obtain SETs with different
properties and SETs possibly working at room-temperature. To the best of our knowledge, our specific approach – chemically connecting Au NPs to Au NRs – have never been used for the purpose of bottom-up fabricated nanoelectronic devices.

Figure 4.10. Differential conductance as a function of bias voltage $V_{bias}$ and gate voltage $V_{gate}$ of a SET fabricated by selective chemical interactions containing 20 nm Au NP ($T<15$ mK) before (a) and after (b) molecular exchange. Inset in (a) shows SEM image of the corresponding device.
REFERENCES


Chapter 5 ELECTRON TRANSPORT THROUGH A PAIR OF METALLIC COULOMB ISLANDS COUPLED IN PARALLEL

This chapter* is dedicated to the investigation of electron transport measurements through a pair of metallic Coulomb islands in parallel. As Coulomb islands we used Au nanoparticles (NPs) embedded between two Au nanorods (NRs). NPs are decoupled from each other and from NRs by molecular barriers (1.8-octanedithiol monolayer). Low temperature measurements reveal single-electron transport through the device which is strongly dependent on the transport through each island. We observed strong cross-talk between islands, which was systematically studied and analysed. We performed numerical simulations supporting our experimental data.

* K.S. Makarenko et al, in preparation
5.1. Double Coulomb Islands Coupled in Parallel

In the previous chapter formation and studying of the individual metallic islands, acting as a single electron transistors (SETs), was described. The next logical step is to study more than one island. By now, electron charge transport through double Coulomb islands in series has been widely investigated [1-14], while the behaviour of parallel Coulomb islands has been studied less [15-19], and to the best of our knowledge has never been shown before for metallic Coulomb islands. The main focus of this chapter is electron transport through a pair of Coulomb islands coupled in parallel (two Au nanoparticles (NPs) between two Au nanorods (NRs), Fig. 5.1) created by means of selective chemical interaction (Chapter 4).

![Figure 5.1. SEM image of the two 20 nm Au NPs enclosed between two Au NRs (~25 nm in diameter and 250 nm long) and schematic of the device.](image)

After the fabrication of the parallel NP system, shown in Fig. 5.1, low-temperature charge transport measurements (<15 mK) have been performed. Figure 5.2 shows the differential conductance ($dI/dV$) of this coupled SET system as a function of the source-drain voltage ($V_{bias}$) and the back gate voltage ($V_{gate}$) applied to the p++ Si substrate, acting as a back gate underneath 35 nm SiO$_2$. 

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Differential conductance $\frac{dI}{dV}$ as a function of the source-drain voltage $V_{\text{bias}}$ and back gate voltage $V_{\text{gate}}$ shows the charge transport through two Coulomb islands in parallel, depicted in Fig. 5.1 (<15 mK).
Figure 5.3. Differential conductance (\(\text{d}I/\text{d}V\)) as a function of the source-drain voltage (\(V_{\text{bias}}\)) and back gate voltage (\(V_{\text{gate}}\)) shows the electron transport through two Coulomb islands in parallel, depicted in Fig. 5.1. Green and blue lines represent Coulomb diamonds of island 1 and island 2. (<15 mK).
5.2. Electron Transport through a Pair of Coulomb Islands Coupled in Parallel

A pair of Coulomb islands coupled in parallel in Fig. 5.1 can be represented as a network of tunnel resistors and capacitors (Fig. 5.4). The number of electrons on island 1 and 2 is \( N \) and \( M \), respectively. Both islands are capacitively coupled to the gate through capacitors \( C_{g1(2)} \) and to the source (s) and drain (d) contacts through tunnel resistors \( R_{s(d)1(2)} \) and capacitors \( C_{s(d)1(2)} \). Islands are also coupled to each other through tunnel resistor \( R_m \) and capacitor \( C_m \).

\[
\Delta V = \frac{e}{C_m} \left( \frac{1}{C_m} - 1 \right)
\]  

Figure 5.4. Schematic of two Coulomb islands in parallel (left) and potential diagrams showing electron transport through parallel islands (right).

In the absence of the tunnel barrier with \( R_mC_m \) between the two Au NPs, the electron transport through one island is independent of the other one, which leads to the superposition of two independent Coulomb diamonds features in the stability plot (\( dI/dV=dI_1/dV+dI_2/dV \) vs. \( V_{gate} \) and \( V_{bias} \)). However, the cross-talk between charges occupying the two islands leads to the complex electron behaviour in Fig. 5.2, and the influence of one electron coming on/off one of the island on the transport of another one can be described as a potential difference [1]:
where \( C_{1(2)} \) is the sum of the capacitances attached to the Coulomb island 1(2).

Charge transport through one island strongly depends on the other one. Corresponding stability diagrams of both islands are depicted in Fig. 5.3 (same as Fig. 5.2 but now with Coulomb diamonds of respective islands indicated). Here, the solid green lines (-----) correspond to the Coulomb diamonds of island 1 when island 2 has a fixed number of electrons \( M \). When island 2 loses/gains one electron \( (M-1/M+1) \), green diamonds shift to the left/right (----------) from the original ones by \( \Delta V \) (Appendix). Losing/gaining two electrons \( (M-2/M+2) \) is leading to the shift of blue diamonds by \( 2\Delta V \) (------), and so on. The same happens with the Coulomb diamonds of island 2 when electrons jumps on/off island 1 (Appendix A).

To clarify the electron transport through the double Coulomb islands in parallel, electrochemical diagrams can be used. Figure 5.5 explains the electron behaviour at zero \( V_{\text{bias}} \) for \(-300 < V_{\text{gate}} < 10 \text{ mV}\). Position (0) depicts a situation when no \( V_{\text{gate}} \) is applied, and islands 1 and 2 have \( N \) and \( M \) electrons, respectively. When a negative \( V_{\text{gate}} \) is applied, the energy levels of the Coulomb islands are pulled up. At position (1) there is an available level \( \mu_1(N,M) \) on island 1, and after crossing this position island 1 has \( N-1 \) electrons. This causes the lowering of the level of island 2 \( \mu_2(N,M) \) to \( \mu_2(N-1,M) \). As a consequence, at position (2), when the applied \( V_{\text{gate}} \) aligns \( \mu_2(N,M) \) to the source/drain, the transport through this level is not possible anymore because the level is not relevant after losing an electron by island 1. At position (3) the transport through island 1 is forbidden since electrons cannot go through the aligned level \( \mu_1(N,M-1) \) due to the fact that island 1 and island 2 have \( N-1 \) and \( M \) electrons, respectively. At position (4) electron transport is possible through island 2 through level \( \mu_2(N-1,M) \).

Current through one tunnel barrier is determined by [20]:

\[
I = \frac{e}{\tau} = e\Gamma \tag{5.2}
\]

where \( e \) is elementary charge, \( \tau \) is the dwell time and \( \Gamma \) is tunnelling rate. In case of the one Coulomb island there are two barriers in series, so the current is given by:

\[
I = \frac{e}{\tau^s_1 + \tau^d_1} = e\frac{\Gamma^s_1 \Gamma^d_1}{\Gamma^s_1 + \Gamma^d_1} \tag{5.3}
\]

where \( \tau^s_1 \) and \( \tau^d_1 \) are the dwell times, and \( \Gamma^s_1 \) and \( \Gamma^d_1 \) are tunnelling rates of the source and drain barriers, respectively; \( i \) is the number of the island (1 or 2).

In Figs. 5.2-5.3, brighter colours correspond to the higher current through islands, which means that the total current through island 2 is
determined by the tunnelling rate of molecular barrier between island 2 and the drain electrode, while charge transport through island 1 is governed by the tunnelling rate of the molecular barrier between island 1 and the source electrode. In other words, island 1 is stronger coupled to the drain, while island 2 to the source electrode (see schematic in Fig. 5.4):

\[
I_1 = e \frac{r_{1s} r_{d1}}{r_{1s} + r_{d1}} \approx e \frac{r_{1s} r_{d1}}{r_{d1}} \approx e r_{1s}, \ (r_{1s} \gg r_{d1}) \tag{5.4}
\]

\[
I_2 = e \frac{r_{2s} r_{d2}}{r_{2s} + r_{d2}} \approx e \frac{r_{2s} r_{d2}}{r_{d2}} \approx e r_{2s}, \ (r_{2s} \ll r_{d2}) \tag{5.5}
\]

**Figure 5.5.** a, Zoom-in of the stability diagram of Fig. 5.3, focused at zero \(V_{\text{bias}}\). b, Schematic diagrams of the electrochemical potentials \(\mu_{1(2)}(N,M)\) in islands and leads for the positions (1)-(6) depicted in a.
Using the schematic stability diagram in Fig. 1.3, it is possible to calculate the coupling and interaction parameters of the two Coulomb islands depicted in Fig. 5.1 (Table 5.1). Based on Table 5.1 and Eq. (5.4)-(5.5) a general schematic electrochemical-potential diagram of the two parallel Coulomb islands can be drawn (Fig. 5.6) and is used to explain the current steps in the experimental data in Fig. 5.2.

**Table 5.1.** Calculation of the coupling and interaction parameters of a pair of Coulomb islands in parallel from Fig. 5.1

<table>
<thead>
<tr>
<th>Island 1</th>
<th>Island 2</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\Delta V_{\text{gate}1} + \Delta V = 230.5$ mV</td>
<td>$\Delta V_{\text{gate}2} + \Delta V = 268$ mV</td>
</tr>
<tr>
<td>$\Delta V_{\text{gate}1} = 185.1$ mV</td>
<td>$\Delta V_{\text{gate}2} = 221.6$ mV</td>
</tr>
<tr>
<td>$\Delta V = 45.4$ mV</td>
<td>$\Delta V = 46.4$ mV</td>
</tr>
<tr>
<td>$\Delta V = 45.9 \pm 0.5$ mV</td>
<td>$\Delta V = e \frac{C_g}{C_g}$</td>
</tr>
<tr>
<td>$\Delta V_{\text{gate}} = 185.1$ mV</td>
<td>$\Delta V_{\text{gate}} = e \frac{C_g}{C_g}$</td>
</tr>
<tr>
<td>slope = $-\frac{C_g}{C_s} = 0.232$</td>
<td>slope = $-\frac{C_g}{C_s} = 0.149$</td>
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<tr>
<td>slope = $\frac{C_g}{C_g + C_d} = 0.141$</td>
<td>slope = $\frac{C_g}{C_g + C_d} = 0.167$</td>
</tr>
<tr>
<td>$C_g = 8.66e^{-19}$ F</td>
<td>$C_g = 7.23e^{-19}$ F</td>
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<tr>
<td>$C_s = 3.73e^{-18}$ F</td>
<td>$C_s = 4.85e^{-18}$ F</td>
</tr>
<tr>
<td>$C_d = 5.28e^{-18}$ F</td>
<td>$C_d = 3.61e^{-18}$ F</td>
</tr>
<tr>
<td>$C_m = 3.49e^{-18}$ F</td>
<td>$\alpha_g = \left(\frac{1}{k_1} + \frac{1}{k_2}\right)^{-1}$</td>
</tr>
<tr>
<td>$\alpha_g = \frac{1}{k_1k_2}$</td>
<td>$\alpha_g = \frac{k_1k_2}{k_1 + k_2}$</td>
</tr>
<tr>
<td>$\alpha_g = 0.088$</td>
<td>$\alpha_g = 0.079$</td>
</tr>
<tr>
<td>$\alpha_g \Delta V_{\text{gate}} = \Delta V_{\text{bias}}$</td>
<td>$\alpha_g \Delta V_{\text{gate}} = \Delta V_{\text{bias}}$</td>
</tr>
<tr>
<td>$\Delta V_{\text{bias}} = 16.3$ mV</td>
<td>$\Delta V_{\text{bias}} = 17.5$ mV</td>
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Electron Transport through a Pair of Coulomb Islands Coupled in Parallel

Figure 5.6. Schematic diagram of electrochemical potentials of a pair of Coulomb islands in parallel at zero $V_{\text{bias}}$ and zero $V_{\text{gate}}$ which can be used to explain any point of the stability diagram in Fig. 5.2.

5.3. Simulation Results

As stated before, when the tunnel barrier with $R_mC_m$ between the two Au NPs is absent, electron transport through one island is independent of the other one, while the presence of a cross-talk between them changes the electron transport dramatically. We show this by numerical calculations, based on the coupling and interaction parameters extracted from the experimental data.
(Fig. 5.2, Table 5.1), using the commercial software SIMON 2.0. A pair of Coulomb islands which are coupled in parallel can be represented as a network of tunnel resistors and capacitors (Fig. 5.4). Simulation results of the electron behaviour through two Coulomb islands in parallel, when islands are not capacitively coupled to each other (Fig. 5.7a), is represented in Fig. 5.8. Here, two sets of diamonds corresponding to two Coulomb islands are independent of each other showing that in the absence of the tunnel barrier between islands the electron transport through one island does not influence the other one. However, Fig. 5.9 shows a remarkable change in the electron transport behaviour when a strong capacitive coupling between Coulomb islands is present (Fig. 5.7b).

Figure 5.7. Network of tunnel resistors and capacitors representing a pair of Coulomb islands in parallel without \( \text{(a)} \) and with \( \text{(b)} \) finite inter-island coupling.

Conclusions

Measurements on double quantum islands in parallel reveal evidence of the interaction between two islands which results in a variety of features in the charge transport spectra. Data analysis and numerical simulations shown that capacitive inter-island coupling leads to the shifting of the regular Coulomb diamonds. The results, represented in this chapter, contribute to the understanding the charge transport behaviour through the hybrid inorganic-organic single-electron transport device containing a pair of interacting Coulomb islands in parallel.
ELECTRON TRANSPORT THROUGH A PAIR OF COULOMB ISLANDS COUPLED IN PARALLEL

Figure 5.8. Simulation of the electron behavior through a pair of Coulomb islands in parallel using a commercial software SIMON 2.0 when transport through each island is independent on each other.
Figure 5.9: Simulation of the electron behaviour through a pair of Coulomb islands in parallel using a commercial software SIMON 2.0 when transport through each island is highly dependent on each other.
REFERENCES


Chapter 6  **Dynamical Nonlocality in a Diffusive Quantum Interferometer**

In this chapter* a Au Aharonov-Bohm (AB) interferometer embedded between two pairs of Au leads (one for the current leads and one for the voltage probes) is employed for a consistent study of the quantum dynamic nonlocality in diffusive system. Here, we perform investigation of the nonlocal signal, and demonstrate that, despite the diffusive motion of electrons, nonlocal quantum correlations can also be observed and controlled in normal metals and be even more pronounced than for ballistic systems. We provide a complete explanation of the nonlocal effect using a simple theoretical model based on the Landauer-Büttiker formalism.

* E. Strambini†, K.S. Makarenko† et al, in preparation
Nonlocality is a key feature discriminating quantum and classical physics. Besides the famous Bell nonlocality [1], allowing for correlations between distant particles stronger than classically possible, the importance of another fundamental quantum nonlocality has been pointed out recently [2, 3]. This dynamical nonlocality follows from the nonlocality of the quantum equations of motion, clearly manifest itself in branching geometries, and is at the base of all quantum interference phenomena, such as, for example, Young’s double slit experiment and the Aharonov-Bohm (AB) effect [4]. Loss of dynamical nonlocality implies quenching of interference. It is well-known that this can occur due to (partial) collapse of the wave function due to a measurement, such as which-path detection [5]. However, other mechanisms affecting dynamical nonlocality have hardly been considered, although of crucial importance in many schemes for quantum information processing. Here, we present a fundamentally different pathway for losing dynamical localization in a solid-state quantum interference experiment where we demonstrate the crucial connection between dynamical nonlocality and the device geometry. We distinguish between the roles of quantum coherence and dynamical nonlocality in a diffusive AB interference experiment, using both local and nonlocal measurement geometries. The nonlocal interference is not only affected by decoherence, but also by a loss of dynamical nonlocality that, in contrast to which-path detection schemes, is based on a local reduction of the number of quantum conduction channels of the interferometer. With our measurements and theoretical model we demonstrate the fundamental nature of this mechanism, which is not limited by the diffusive transport regime, nor by the specific quantum wave-particle used (in our case electrons). Understanding the geometrical constraints protecting this kind of nonlocality is crucial when designing quantum networks for quantum information processing.

The AB effect [4] is one of the most intriguing and insightful phenomena in quantum mechanics. If a quantum mechanical wave function, e.g. describing a propagating electron, is spatially split to enclose a region of magnetic flux, a phase difference develops, leading to quantum interference oscillations periodic in the magnetic flux quantum, $h/e$ ($h$ is the Plank’s constant and $e$ is the elementary charge). The AB effect has been experimentally demonstrated in a large number of systems, ranging from electron microscopy experiments [6, 7] to electron transport in mesoscopic rings [8-12]. As for the latter, the AB effect has been shown both in the diffusive [8, 9] and ballistic [10-12] regime with an oscillation amplitude of the order $e^2/h$, corresponding to the contribution of a single quantum conduction channel. It is remarkable that the AB effect survives in metallic rings where, despite the many conduction channels and (elastic) scattering events, its amplitude remains of the same order. The AB effect not only nicely
demonstrates single electron interference, it also allows one to determine the electron coherence length \(l_\varphi\) [13]. In this chapter, we present a set of electron-interference experiments in which besides the effect of decoherence we also observe the effect of loss of dynamical nonlocality [2, 3]. The dynamical nonlocality of electrons traversing the AB ring, induced by the branching of the conduction path, is, together with quantum coherence, the basic ingredient of the AB effect and, in fact, of any interference phenomenon.

Loss of dynamical nonlocality has been first demonstrated and tuned in which-path experiments [5, 14], one of the most remarkable manifestations of the complementarity principle. In these experiments, detection of the photon, respectively electron, traversing the two branches of the interferometer induces a collapse of the delocalized quantum state (wave-like) in a localized one (particle-like), resulting in quenching of the interference.

Here we investigate a new phenomenon affecting the dynamical nonlocality that, different from the which-path scheme, is inherent to the device geometry and originates from a reduction of the number of conduction channels instead of from the interaction with the external environment described above. This loss of dynamical nonlocality is not observed in a regular, local AB measurement geometry, but does play a significant role in the nonlocal geometry. In the nonlocal geometry, also the quantum nature of the side arms of the ring is crucial, as opposed to the local geometry, where only the ring itself matters. In the side arms, conduction channels can directly interact and merge, which is prevented in the ring. The implication of this fundamental difference will be discussed in detail below.

6.1. Dynamic Nonlocality in a Diffusive Aharonov-Bohm Interferometer

Figure 6.1a shows an image of a representative Au AB interferometer. More than ten devices of different size exhibited similar behaviour (Section 6.4). The AB ring is connected to two \(\sim 100\) nm long side arms, which each splits into two leads. This device layout allows for measuring the differential resistance \(dV_L/dI=R_L\)\(\sim 14,23\), current: \(1\rightarrow 4\), voltage: \(2\leftrightarrow 3\) in the conventional, local configuration (red, upper diagram in Fig. 6.1a). The local signal represented in the upper panel of Fig. 6.1b shows clear AB oscillations, see Fig. 6.1c, superimposed on a reproducible background of universal conductance fluctuations (UCF) (Section 1.2) [15]. The corresponding Fourier spectrum (Fig. 6.1d) clearly reveals the AB period \(h/e\), as well as higher harmonics up to \(h/4e\). In addition to \(R_L\), we have also measured the nonlocal differential resistance \(dV_{NL}/dI=R_{NL}\)\(\sim 12,34\), according to the scheme in the lower, blue
Classically, one expects to measure a zero signal in this configuration (or exponentially small according to the Van der Pauw theorem [16]). However, in the quantum coherent transport regime, the signal may be nonzero [15, 17] as the electron wave function, dynamically delocalized in the system, can connect the current and voltage probes within a distance of a few coherence lengths. Indeed a nonlocal AB effect has recently been measured in ballistic rings [18-22].

Figure 6.1. a, AFM image of the Au AB interferometer and schematics of two measurement configurations: local 4-terminal (current: 1→4, voltage: 2↔3) and nonlocal 4-terminal (current 1→2; voltage 3↔4). b, MR of the ring in a measured in local (red) and nonlocal (blue) geometries. c, Zoom-in of the magneto-resistance represented in b. d, Fourier transform of the data in a. The bounds for the flux periods $\hbar/ne$ ($n = 1, 2, 3, 4$) are calculated based on the inside and outside circumference of the device. (40 mK, 30 nA ac excitation current).

To the best of our knowledge, nonlocal AB oscillations have never been observed in diffusive, metallic rings. We do, however, observe very clear
nonlocal AB oscillations (Fig. 6.1b, blue) superimposed on reproducible fluctuations (UCF) around a zero average (Fig. 6.1c, blue). The Fourier spectrum shows the same four harmonics as for the local signal, but with roughly half the amplitude (Fig. 6.1d, lower panel).

For both the local and nonlocal configurations the amplitude of these Fourier peaks follows a clear exponential decay in the harmonic index $n$ (as shown in the insets of Fig. 6.1d), as the path length scales with $n$, corresponding to the number of times that the electron encloses the ring. This decay thus provides a direct measure of the electron coherence length $l_{\varphi}$ [13]. Using the power law $e^{-0.6nC/l_{\varphi}}$, expected for a diffusive interferometer [17], where $C$ is the ring circumference, giving rise to $l_{\varphi}=\sim1.5 \ \mu m$ for both the local and nonlocal configurations. The value of $l_{\varphi}$ is consistent with values found from weak localization and UCF measurements in mesoscopic Au structures at millikelvin temperatures [23]. Other similar rings show the same trend with $l_{\varphi}=1-2 \ \mu m$ (Section 6.4), independent of sample size and temperature below 1 K, as expected for gold [24]. Our results demonstrate that both the local and nonlocal interference are equally suppressed by decoherence inside the ring. Decoherence inside the side arms is only relevant for the nonlocal signal, leading to an additional damping $e^{-1.1d/l_{\varphi}}$ [17], where $d$ is the total length of the side arms. As a consequence, the amplitude of the nonlocal AB oscillations is smaller than that of the local AB oscillations, as seen in Fig. 6.1d. This is in agreement with other studies on nonlocal interference [15, 18, 25].

6.2. Local and Nonlocal Measurements in the Multi-Terminal Quantum Interferometer

To study the damping effect of the side arms on the nonlocal AB oscillations in more detail, we measured $R_{NL}$ and $R_L$ in the multi-terminal interferometer shown in Fig. 6.2a, in which the side arm length $d$ can be varied (Fig. 6.2c,d). Clear AB oscillations are visible for $d=100 \ \text{nm}$ in both $R_L$ ($R_{09,14}$ red plot in Fig. 6.2e) and $R_{NL}$ ($R_{12,34}$ blue plot in Fig. 6.2f). For $R_L$ the amplitude of the AB oscillations does not significantly change when the arm length $d$ is increased, see Fig. 6.2b. By contrast, the amplitude of the nonlocal AB oscillations is strongly suppressed with increasing $d$. The damping of the nonlocal oscillations can be described by the power low $e^{d/\xi}$, see Fig. 6.2b, where $\xi\sim350\pm50 \ \text{nm}$ is the characteristic length scale of the damping. Interestingly, this damping is about three times faster than the theoretical expectation for a nonlocal measurement [17], which would give a value of $\sim1.5 \ \mu m$. We ascribe this large discrepancy to a loss of dynamical delocalization in the nonlocal geometry.
Figure 6.2. a, AFM image of the multi-terminal Au AB interferometer. b, Dependence of the quantum resistance oscillations on the distance $d$ between the probes and the ring showing the damping of the nonlocal voltages with increasing $d$. The amplitude of the quantum resistance oscillations and the error bars are determined from the Gaussian fit of the first peak in the Fourier transform of the data in e and f. c-d, Schematics of the local and nonlocal measurement geometries. e-f, Quantum resistance oscillations measured in local and nonlocal geometries.

Inside the AB ring itself merging of conduction channels in different branches of the ring is impossible, as they are simply spatially separated and therefore perfectly dynamically delocalized. In the local AB effect, loss of
dynamical delocalization associated with merging of conduction channels inside the arms leading to the ring does not have any effect on the AB amplitude, because only the ring itself is relevant for the interference. However, in the nonlocal AB effect, reduction of the amount of conduction channels inside the side arms has profound consequences for the interference, as follows straightforwardly from the model introduced below.

6.3. Analytical Model Explaining the Nonlocal Effect*

We use the Landauer-Büttiker (LB) formalism [26] to catch the essential physics that describes this quenching of interference in the nonlocal experiments first in the few-channel regime, and then extend the argument to our multichannel diffusive experimental system.

In the LB formalism the transport properties of a 4-terminal device are completely described by a unitary $4 \times 4$ scattering matrix $t_{ij}$ representing the amplitude probabilities for an electron injected in the terminal $i$ to be transmitted to terminal $j$.

According to the scheme in the inset of Fig. 6.3a, the scattering matrix of a 4-terminal AB interferometer (without side arms) can be obtained by combining the scattering matrices of two $4 \times 4$ side nodes with a $4 \times 4$ phase-shifter representing the two branches of the ring, each of them shifting the electron phase by $\pm \phi/2$, where $\phi$ is the AB phase. The 4-terminal resistances $R_{nm,kl}$ (current: $n \rightarrow m$, voltage: $k \rightarrow l$) are then extracted from the coefficients of the probability matrix $T_{ij} = |t_{ij}|^2$ according to the LB analytical formula [26]:

$$R_{nm,kl} = \frac{\hbar^2 e^2}{2}\frac{(T_{km}T_{ln}-T_{km}T_{ln})}{D}$$

(6.1)

where $D$ is a quantity including all of the $T_{ij}$’s coefficients.

Assuming a symmetric splitting probability in the two branches of the ring (Fig. 6.3a) and an exponential damping of the amplitude ($e^{-C/\phi}$) in both branches of the ring, to simulate decoherence, we obtain the $R_L$ vs. $\phi$ and $R_{NL}$ vs. $\phi$ plots shown in Fig. 6.3b. This single-channel model describes the fundamental characteristics of the experimentally observed $R_L$ and $R_{NL}$ well: a positive $R_L$ exhibiting AB oscillations, and an $R_{NL}$ oscillating between positive and negative values with a similar amplitude $\Delta R_L \sim \Delta R_{NL}$. This picture changes drastically when modelling the same ring with additional side arm, as represented in Fig. 6.3c. The addition of the single-channel side arm results in the complete quenching of all $R_{NL}$, while the behaviour of $R_L$ is not strongly affected, see Fig. 6.3d.

*The model was developed by Elia Strambini
Figure 6.3. Consequence of the reduction of the amount of quantum channels in the side arm. a, Scheme of the simple 4-terminal AB interferometer with a detailed representation of the second node of the interferometer in which the two electronic paths of the ring (green and blue arrows) interfere generating the two phase-correlated output channels represented by the red arrows (solid and dashed). b, Comparison between the 4-terminal local (red) and nonlocal (blue) resistances simulated as a function of the magnetic AB phase $\phi$ for an AB ring without side arms. c, Scheme of the 4-terminal AB interferometer with one side arm allowing a reduction of two conduction channels into one after the characteristic distance $L^*$ and leading to quenching of the phase correlation between the two electronic paths of the ring, resulting in two phase-uncorrelated output channels represented by the solid red arrows. d, Comparison between the 4-terminal local (red) and nonlocal (blue) resistances simulated as a function of the magnetic AB phase $\phi$ for the AB ring with side arms.
This detrimental effect on the nonlocal signal when forcing the conduction channels of both branches of the ring into the single channel of a side arm provides a strong clue for explaining the experimentally observed suppression of the AB oscillations in the nonlocal geometry. The forced reduction in the amount of conduction channels when the branches of the ring come together in the side arm generates an intrinsic constraint among the transmission coefficients representing the electrons injected in the side arm (e.g., $t_{13}, t_{14}, t_{23}, t_{24}$ in the schematic of Fig. 6.3c). The simple relation $t_{13}t_{24} = t_{23}t_{14}$ holds, independent of the complexity or asymmetry of the system. From the definition of the 4-terminal resistance (Eq. 6.1), it is straightforward to note that this geometrical constraint is the origin of the quenching of all the nonlocal resistances (e.g., $R_{NL} = R_{43,12} = T_{13}T_{24} - T_{14}T_{23} = 0$), while it is only weakly affecting the local one. This geometrical effect and the corresponding quenching of $R_{NL}$ reduces if the side arms are composed of more than a single conduction channel, as is expected in the diffusive case. This model is in agreement with experimental observations of the nonlocal AB effect in ballistic systems [18-22], in which the nonlocal AB oscillations have been reported for several transport channels. In our metallic devices, the side arms are composed of a multitude of interacting channels due to the diffusive electron motion, and the probability that scattering merges two otherwise distinct conduction channels into a single one (event represented in the scheme of Fig. 6.3c) is very high. The measured signal comes from the average of all the possible diffusive electron paths, in this average the paths that experience such a reduction do not contribute to interference, as demonstrated in our model. Due to the random distribution of electron paths in a diffusive metal, the probability for this event to occur is expected to scale exponentially with the length of the side arm ($\propto 1 - e^{-d/L^*}$, where $L^*$ is the characteristic length of this event) and as a consequence the nonlocal signal is damped within the same length scale ($e^{-d/L^*}$) and additionally to the damping induced by decoherence [17]. This behaviour is in agreement with the strong exponential damping of the $R_{NL}$ shown in Fig. 6.2c from which we can estimate $L^* = (1/\xi - 1.1/l_{\phi})^{-1} \approx 450 \pm 50$ nm.

6.4. Characterisation of Aharonov-Bohm Interferometers

6.4.1. Evaluation of the Coherence Length

Figure 6.4 shows the fast Fourier transform (FFT) of the magneto-resistance oscillations measured through the device in Fig. 6.1a in the local and the nonlocal configurations, after subtracting a polynomial fit (to remove the
aperiodic background fluctuations, UCF). Six clear peaks corresponding to the $h/ne$ harmonics can be observed.

The amplitude of the AB oscillations decays exponentially with the coherence length of the system according to these relations [17]:

for $R_L$:

$$A \propto e^{-0.6 \frac{nC}{l_\phi}},$$  \hspace{1cm} (6.2)

for $R_{NL}$:

$$A \propto e^{-\left(0.6 \frac{nC}{l_\phi} + 1.1 \frac{d}{l_\phi}\right)},$$  \hspace{1cm} (6.3)

where $C$ is the circumference of AB interferometer, $d$ is the total length of the side arms, $l_\phi$ is coherence length. Based on Eqs. (6.2)-(6.3) we can extract $l_\phi$ by fitting the peak amplitude in the Fourier transform (see insets of Fig. 6.4a,b). We obtained a coherence length $l_\phi$ of $\sim 1.5$ µm for both local and nonlocal configurations.

![Figure 6.4. Characterisation of Au AB interferometer. a, Representative FFT of $R_{NL}$ of the interferometer in Fig. 6.1a, showing up to six harmonics. b, FFT peak amplitudes of the magneto-resistance, represented in Fig.1b, vs. harmonic index $n$. Inset in b shows FFT peak amplitude of the $R_{NL}$ vs. $n$ characteristic of the Au AB interferometer shown in Figs.2d (40 mK, 30 nA ac excitation current).](image)

### 6.4.2. Temperature Dependence of the AB Oscillation Amplitude

Temperature dependence of the AB oscillation amplitude (Figs. 6.5) shows that although the amplitude of the FFT peaks decreases, the ratio between the different harmonics remains almost the same. From this ratio the coherence length can be extracted. We observed that despite the constant coherence length below 1 K (Fig. 6.6) the amplitude of the oscillations is damping what can be addressed to a phase averaging due to the thermal broadening.
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Figure 6.5. Temperature dependence of the AB oscillation amplitude: dependence of the $h/e$ oscillations for the local (a) and the nonlocal (b) geometries (30 nA ac excitation current).

Figure 6.6. Temperature dependence of the coherence length of the AB interferometer in Fig. 6.1a: for the local (a) and the nonlocal (b) configurations (30 nA ac excitation current).

6.4.3. Excitation Current Dependence of the AB Oscillation Amplitude

Figure 6.7 shows an excitation current ($I_{ac}$) dependence of the AB oscillation amplitudes for the 1$^{st}$, 2$^{nd}$ and 3$^{rd}$ FFT peaks, measured in the local configuration. The amplitude of the FFT peaks does not change for excitation
currents below $\sim 50$ nA (see the crossing point of two red dashed guiding lines in Fig. 6.7). From this $I_{sc}$ value and the AB ring’s resistance ($\sim 282$ Ω) the corresponding energy broadening is $\Delta E \sim 14$ μeV from which it is possible to estimate an effective electron temperature $T_e \approx 50$ mK ($\Delta E = 3.5 kT_e$). Above this point the peak amplitudes decay due to phase averaging or heating induced by the excitation current.

![Figure 6.7](image)

**Figure 6.7.** Excitation current dependence represents damping of the 1st, the 2nd and the 3rd FFT peaks of the AB oscillations measured for the AB ring in Fig. 6.1a in the local configuration (T=40 mK).

### 6.4.4. Size Dependence of the AB Oscillations

The AB period is determined by the ring’s enclosed area $S_{in}$, $\Delta B = h/eS_{in}$ [4]. Figure 6.8 shows electrical measurements on two AB interferometers of a different size (490±10 (Figs 6.8a,b in black) and 590±10 nm (Figs 6.8a in red, Fig. 6.8b, in blue)) in diameter) for local (Fig. 6.8a) and nonlocal (Fig. 6.8b) configurations. Calculated from the geometry of the AB rings oscillation frequencies $1/\Delta B = e/hS_{in}$ are $(52 \pm 2)$ and $(75 \pm 2)$ T$^{-1}$ for the (490±10) and (590±10) nm diameter interferometers, respectively, are in agreement with extracted from FFT peaks AB period of $\sim 51$ and $\sim 74$ T$^{-1}$ (for 490 and 590 nm, respectively) (Figs. 6.8c,d).
Conclusions

We have thus shown a new aspect of the dynamical nonlocality of electrons in a quantum circuit that is solely governed by geometric aspects and not by external measurement. Understanding this geometrical constraint is essential for the optimal design of any quantum circuit based on the dynamical nonlocality of the electrons. Moreover, as deduced from our model, the strong link between geometry and nonlocality is a universal property of quantum dynamics not limited by the diffusive transport regime of our experiment, nor by the specific quantum wave-particle used (in our case electrons). We believe that these results will trigger further investigation of the fundamental properties of quantum dynamics and of its application in quantum information processing.
REFERENCES


This chapter is dedicated to the experimental observation of potentially coherent electron transport through molecular layers. In an Aharonov-Bohm (AB) interferometer based on a pair of Au nanoparticles (NPs) coupled in parallel between two Au nanorods (NRs), we show an indication of the coherent electron transport through 1,8-octanedithiol self-assembled monolayers (SAMs). Based on the obtained result, we propose novel geometries for hybrid AB interferometers containing embedded molecular barriers, which may allow for a consistent study of coherent electron transport through molecules.
7.1. Coherent Transport through Organic Molecular Layers

Although coherent electron transport in inorganic systems is experimentally well studied by now [1-4], the coherence of electron transport through organic molecules is experimentally much less explored [5-9]. Understanding the transport through molecular systems has attracted considerable interest due to their potential application in nanoelectronics. It is a fair and fascinating question to ask to what extent transport through organic molecules is coherent and how the coherence depends on the molecule’s characteristics (e.g. length, chemical composition, side groups, chemical bonding), as well as on external parameters (e.g. temperature, electrostatic potential, magnetic field). Our objective is to include monolayers of organic molecules in electron interferometer geometry, allowing for a systematic study of charge coherence in molecular systems.

7.2. Aharonov-Bohm Oscillations in Gold Rings Bridged by Gold Nanoparticles

The first step towards studying interference effects in hybrid inorganic-organic AB interferometer is to show coherent transport through a bottom-up AB interferometer without molecular junctions (so in fully inorganic structures). Using dielectrophoresis (DEP), described in chapter 2, we bridged 30 nm gaps in Au AB interferometer with a diameter of 500 nm by a few non-functionalised (“naked”) Au NPs, which are on average 20 nm in diameter (inset in Fig. 7.1).

Figure 7.1 shows clear AB oscillations in a magnetic field between 6 and 6.5 T, measured in a four-wire configuration. The Fourier transform of these oscillations, after subtracting a polynomial fit (to remove the background fluctuations, UCF (Section 1.2)), is shown in Fig. 7.2, where three clear peaks at 50 T⁻¹, 102 T⁻¹ and 150 T⁻¹ can be observed, which correspond to the first \( \frac{h}{e} \), the second \( \frac{h}{2e} \) and the third \( \frac{h}{3e} \) harmonics. From these equidistant FFT peaks the AB period \( \Delta B \) is estimated to be 20 mT, in good agreement with the calculated period of \((19\pm2)\) mT for the geometry of the measured ring. The widths of the \( \frac{h}{e} \), \( \frac{h}{2e} \) and \( \frac{h}{3e} \) are calculated from the ring’s aspect ratio and are indicated by bars in Fig. 7.2.

This experimental observation of AB oscillations in Au rings realized by combining bottom-up (self-assembly of NPs) and top-down (electron beam lithography) approaches (inset in Fig. 7.1) suggests that the proposed novel hybrid Au AB ring (see below, Section 7.4) can be used to probe the coherent electron transport properties of the organic molecules of interest.
Figure 7.1. AB oscillations observed in a 500 nm diameter Au AB ring (AFM image in the inset), closed by few 20 nm diameter non-functionalised Au NPs, bridged via DEP (black line), and polynomial fit of the data (red line) (32 mK, 50 nA ac excitation current at 17.7 Hz).

Figure 7.2. Fourier transform of the AB oscillation in Fig. 7.1, after subtracting the polynomial fit. The bars to each peak indicate the frequency bandwidth for $\hbar/e$, $\hbar/2e$, and $\hbar/3e$ oscillations. The inset shows AFM image of the measured ring.
7.3. Interference Effects in Aharonov-Bohm Ring Created via Selective Chemical Interaction

Two Au NPs assembled in parallel between two Au nanorods (NRs) (Chapters 4-5) and decoupled from them by a molecular barrier (1,8-octanediol) form a branching geometry that could possibly act as a two-path interferometer. Figure 7.3 shows a scanning electron microscopy (SEM) image of the device.

![Figure 7.3](image)

**Figure 7.3.** SEM image of the two 20 nm Au NPs enclosed between two Au NRs (~25 nm in diameter and 250 nm long) (Chapters 4-5). The inset shows schematic of the device which may act as an AB interferometer.

Figure 7.4 shows the differential conductance \((dI/dV)\) through the device in Fig. 7.3 as a function of the source-drain voltage \((V_{\text{bias}})\) and back gate voltage \((V_{\text{gate}})\). When an electron is able to move simultaneously through both branches of the AB interferometer, the AB effect may be observed. For our device (Fig. 7.3) this condition will be fulfilled when both dots are out of the Coulomb blockade region. In chapter 5 we have discussed that electron transport through one Coulomb island strongly depends on the transport through the other island coupled in parallel. Therefore, we carefully chose the position inside the stability diagram (Chapter 5, Figs. 5.3-5.6). Figure 7.5 shows conductance oscillations in a magnetic field piercing the device. These oscillations are reproducible in time and were tested for a different step sizes of the magnetic field sweep to exclude spurious effects. The inset in Fig.7.5
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shows a dummy time sweep where no oscillations are present. This suggests that the observed periodic magnetic field dependence (yellow dashed sine curve fit in Fig. 7.5) is caused by interference of electrons traversing the device.

The inset in Fig. 7.4 shows a schematic diagram of the electrochemical potentials $\mu_{1(2)}(N,M)$ (Section 1.3) in the islands and leads for the chosen optimal configuration, at which electrons can traverse both islands.

Figure 7.4. a, Differential conductance ($dI/dV$) as a function of the source-drain voltage ($V_{\text{bias}}$) and back gate voltage ($V_{\text{gate}}$), showing electron transport through a pair of Coulomb islands in parallel, depicted in Fig. 7.3. The inset in a shows a zoom-in of the chosen measurement region (high-lighted by the white circle). b, Stability diagram showing electrochemical potentials $\mu_{1(2)}(N,M)$ corresponding to two Coulomb islands (Section 1.3) at the chosen region in the inset in a (Section 5.2). (T< 15 mK)

We also observe a change of the magnetic field oscillations for different gate and bias voltages (Figs 7.6 and 7.7, respectively). Such
behaviour was observed in metal AB rings containing tunnel barriers in its branches and may be addressed to the electric modification of the electron phase [4].

**Figure 7.5.** Conductance oscillations through the double Coulomb islands coupled in parallel, shown for different step sizes and directions of the magnetic field sweep. Yellow dashed line is sine curve fits. Inset: dummy time sweep showing no periodic oscillations. ($V_{bias}=13$ mV, $V_{gate}=-190$ mV, $V_{AC}=100$ µV at 17.7 Hz, $T=30$ mK).

**Figure 7.6.** Conductance oscillations at different gate voltages ($V_{gate}$) showing a change in the behaviour for the fixed bias and excitation voltages ($V_{bias}=13$ mV, $V_{AC}=100$ µV at 17.7 Hz, $T=30$ mK).
Figure 7.7. Conductance oscillations at different bias voltages ($V_{\text{bias}}$) showing a change in the behaviour for the fixed gate and excitation voltages ($V_{\text{gate}}=-190$ mV, $V_{\text{AC}}=100$ µV at 17.7 Hz, $T=30$ mK).

Figure 7.8. Schematics of the devices in Fig. 7.3 showing possible origin of the observed periodic oscillations in Fig. 7.5-7.7: UCF in leads and NRs (a), in a single Au NP (b), in areas containing single Au NP and molecular junction(s) (c); AB effect (d).
From the test measurements in Fig. 7.5 we may conclude that the observed interference effects are caused by the magnetic field piercing the device. There are two well-known interference effects at the mesoscopic scale: UCF and the AB effect (Sections 1.1-1.2). Figure 7.8 suggests the four possible scenarios which might cause oscillations in Figs. 7.5-7.7: 1 – UCF in leads and NRs (Fig. 7.8a); 2 – UCF in a single Au NP (Fig. 7.8b); 3 – UCF in areas containing a single Au NP and molecular junction(s) (Fig. 7.8c); 4 – AB effect (Fig. 7.8d). The period of observed oscillations $\Delta B$ varies between ~4-6 T which corresponds to the enclosed area $S_{in}=(8.6\pm1.8)\cdot10^{-16}$ m$^2$ (assuming the circular area, the corresponding diameter is 23.3±2.4 nm) for the AB effect and/or UCF for devices with small dimensions ($\ll l_\varphi$, where $l_\varphi$ is the phase coherence length, which is in order of 1-2 µm for gold [10]). Oscillations caused by UCF in NRs and leads (Fig. 7.8a) are expected to have much bigger $S_{in}$ and, therefore, much smaller $\Delta B$ (see Section 1.2).

Figure 7.9 schematically represents the current circuit through the Au NR – molecular layer – Au NP – molecular layer – Au NR junction. Assuming that the observed oscillations are due to the interference effects in the metallic parts of the device, the visibility of the quantum oscillations (determined by the ratio of the oscillation signal to the main signal) would be:

$$\frac{\Delta R}{R_\Sigma} = \frac{\hbar/e^2}{R_{NR1}+R_{mb1}+R_{NP}+R_{mb2}+R_{NR2}} \approx \frac{\hbar/e^2}{2R_{mb}} = 0.4\% \quad (7.1)$$

assuming that $R_{Au} = R_{NR1} = R_{NR2} = R_{NP} =$ a few $\Omega$ and $R_{mb} = R_{mb1} = R_{mb2} =$ 3.2 M$\Omega$, where $\Delta R = \hbar/e^2 \approx 25$ k$\Omega$ is the quantum resistance, $R_\Sigma$ is the total resistance through the system, $R_{NR1}$, $R_{NR2}$, $R_{NP}$, $R_{mb1}$, $R_{mb2}$ and $R_{Au}$ are resistances of the first NR, the second NR, NP, the first molecular barrier, the second molecular barrier and gold, respectively. While the observed oscillations in Figs. 7.5-7.7 are ~10% of the main signal. This is an indication that the observed amplitude of the oscillations is not due to the interference effects in the isolated metallic parts of the device, excluding options a n b in Fig. 7.8, but more likely due to the presence of the tunnel barriers incorporated in the system [4].

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7.4. Hybrid Aharonov-Bohm Interferometers: Perspectives

In this chapter we have shown that interference effects can be observed in inorganic bottom-up Au AB interferometers, and possibly also in hybrid inorganic-organic systems. The next step is to fabricate a hybrid AB interferometer (where UCF and AB effect can be distinguished) with embedded molecular junctions in order to demonstrate coherent electron transport through organic materials. Figure 7.10 shows some proposed geometries for hybrid inorganic-organic AB interferometers.

An Au ring containing gaps functionalized with a desired SAM and bridged by Au NPs via DEP (Fig. 7.10a) is a good candidate for the hybrid inorganic-organic AB interferometers to study coherence in molecular layers. The main disadvantage of such interferometers is that at low temperatures, when interference effects are studied, electron transport is suppressed due to the Coulomb blockade in Au NPs acting as Coulomb islands which provides extra complications during measurements. To overcome the blockade one may study the interference effects in hot electrons by applying a bias voltage over the AB interferometer or adding side gates to independently control the Coulomb blockade of the dots. The AB effect has been exploited to demonstrate that electron tunnelling through a semiconductor quantum dot embedded in one arm of an AB ring is at least partly coherent [11, 12]. A number of samples was tested. We measured clear UCF, but we did not observe an indication of the AB effect. It is possible that NP(s) in one branch of the ring is(are) coupled stronger to the leads than NP(s) in the other arm which may lead to conductance mostly through one branch of the AB interferometer suppressing AB effect. We cannot demonstrate that NPs in both branches are touching the leads properly.

Coulomb blockade is a smaller issue in the AB rings fabricated using the wedging transfer technique (Fig. 7.10b). As discussed in chapter 3, besides the negligible effect of the Coulomb blockade molecular junctions created via wedging transfer method provide higher conductance (see Section 3.4) which may become a big advantage. Nevertheless, the alignment between the bottom and the top (transferred) electrodes is still a challenge. Figure 7.10c shows a proposed design of a hybrid AB ring (yellow and orange areas represent bottom and top electrodes, respectively) where the alignment problem is solved and by different ways of electrical contacting the number of molecular junctions in a device can be varied. Due to the low yield of the wedging transfer technique (Chapter 3), we did not succeed in the fabrication of hybrid AB rings with a reasonable conductance for molecular junctions ($<e^2/h$) (Section 1.4).
In chapter 4 we have shown that by selective chemical interactions Au NPs can be attached to Au NRs. We proposed to use the same technique to fabricate a hybrid AB interferometer by contacting NR-NR assemblies (Fig. 7.10d). The technique was shown to be very reproducible with a high yield (>50%) and by exclusion of NPs from the assembly we avoid Coulomb blockade regime at low temperatures. In a few rings we observed strong UCF signal but no AB oscillations were present.

**Figure 7.10.** AFM and scanning electron microscopy images showing examples of the modified hybrid inorganic-organic AB interferometers fabricated via (a) DEP, (b-c) wedging transfer technique and (d) bottom-up assembled Au NRs assemblies. **C.** The design of the modified AB interferometer made via wedging transfer technique, where yellow and orange areas represent bottom and top (transferred) electrodes, respectively.
Conclusions

We demonstrated the experimental observation of the AB effect in an Au interferometer realized using the DEP method. Electrical measurements in a magnetic field through a pair of Coulomb islands in parallel decoupled from each other and from the Au NRs by a dithiol molecular layer reveal interference effects that might be addressed to the AB effect and as a consequence to coherent transport through the molecular layer. We proposed a few methods to fabricate hybrid inorganic-organic AB interferometers where molecular layers of interest can be embedded for the consistent study of the coherent electron transport. The results suggest that the proposed novel hybrid Au AB interferometers are good candidates for a test-bed for studying coherent electron transport properties of organic molecules.

REFERENCES


Appendix A

Stability Diagrams of
Single-Electron Transport through a
Pair of Coulomb Islands Coupled in Parallel
Figure 0.1. Differential conductance ($dI/dV$) as a function of the source-drain voltage ($V_{\text{bias}}$) and back gate voltage ($V_{\text{gate}}$) shows electron transport through a pair of Coulomb islands in parallel, depicted in Fig. 5.1. Green and lines represent Coulomb diamonds of island 1 when island 2 has $M$ electrons. (<15 mK).
Figure 0.2. Differential conductance ($dI/dV$) as a function of the source-drain voltage ($V_{\text{bias}}$) and back gate voltage ($V_{\text{gate}}$) shows electron transport through a pair of Coulomb islands in parallel, depicted in Fig. 5.1. Green and lines represent Coulomb diamonds of island 1 when island 2 has $M-1$ electrons. ($<15$ mK).
Figure 0.3. Differential conductance \( \frac{dI}{dV} \) as a function of the source-drain voltage \( V_{\text{bias}} \) and back gate voltage \( V_{\text{gate}} \) shows electron transport through a pair of Coulomb islands in parallel, depicted in Fig. 5.1. Green and lines represent Coulomb diamonds of island 1 when island 2 has \( M-2 \) electrons. (\(<15 \text{ mK}\).)
Figure 0.4. Differential conductance ($dI/dV$) as a function of the source-drain voltage ($V_{\text{bias}}$) and back gate voltage ($V_{\text{gate}}$) shows electron transport through a pair of Coulomb islands in parallel, depicted in Fig. 5.1. Blue lines represent Coulomb diamonds of island 2 when island 1 has $N$ electrons. ($<15$ mK).
Figure 0.5. Differential conductance ($dI/dV$) as a function of the source-drain voltage ($V_{\text{bias}}$) and back gate voltage ($V_{\text{gate}}$) shows electron transport through a pair of Coulomb islands in parallel, depicted in Fig. 5.1. Blue lines represent Coulomb diamonds of island 2 when island 1 has $N-1$ electrons ($<15$ mK).
Figure 0.6. Differential conductance ($dI/dV$) as a function of the source-drain voltage ($V_{\text{bias}}$) and back gate voltage ($V_{\text{gate}}$) shows electron transport through a pair of Coulomb islands in parallel, depicted in Fig. 5.1. Blue lines represent Coulomb diamonds of island 2 when island 1 has $N-2$ electrons. ($<15 \text{ mK}$).
Summary

Charge Transport in
Bottom-Up Inorganic-Organic and
Quantum-Coherent Nanostructures

This thesis is based on results obtained from experiments designed for a consistent study of charge transport in bottom-up inorganic-organic and quantum-coherent nanostructures. New unconventional ways to build elements of electrical circuits (like dielectrophoresis, wedging transfer and bottom-up fabrication using selective chemical interactions) were studied and are presented in this thesis. We also investigated the next steps in understanding fundamental physics phenomena such as charge transport through a pair of metallic Coulomb islands coupled in parallel, coherent transport through organic molecular monolayers and dynamical nonlocality in normal metals.

Dielectrophoresis (DEP) and wedging transfer are top-down techniques which allow soft-contacting of electrodes covered by self-assembled molecular monolayers (SAMs) without damaging it, leading to the formation of the ~1-2 nm wide molecular tunnelling junctions avoiding the requirement for the creation of extremely small nanogaps. DEP is a high-yield, simple and reproducible processing technique that is a good alternative top-down technology for building of molecular bridges. This method allows not only characterisation of a large number of molecular monolayers, but also fabrication of single-electron transistors (SETs) by trapping a single nanoparticle (NP) (metallic or semiconducting) between source, drain and gate electrodes and decoupling the NP via molecular barriers. Wedging transfer is a promising alternative method for the fabrication of nano- and micro-sized area molecular junctions. However, the low-yield of the working devices fabricated by means of wedging transfer indicates the necessity of further improvement of the fabrication process.

The study of molecular SAMs (Chapters 2,3) shows that electron transport through alkanedithiols is typical of non-resonant tunnelling, independent of the temperature or external magnetic field. However, the molecular length as well as the molecular composition strongly affect the
conductance through molecules. As predicted, alkanedithiols are more resistive than π-conjugated molecular monolayers.

On-going miniaturization of silicon transistors over the last few decades, driven by scientific and technological innovations, is enabled by developments in top-down fabrication methods. Nevertheless, approaching of crucial features below ~10 nm makes top-down methods more challenging and costly. This raises the interest in the investigation of a new unconventional way of realizing functional nanoelectronic devices. In chapter 4 a bottom-up approach for fabrication of SETs based on single ~20 nm Au NP is exploited. We successfully combined self-assembly of an Au NP to Au nanorods (NRs) with top-down lithography. Low-temperature electrical measurements of the electron transport through the SETs revealed clear signatures of the classical Coulomb blockade regime. The fabrication process shows very high reproducibility (>50%) and the SETs are very stable over a few months. Both the temperature and size dependence are in good agreement with theoretical predictions.

Electron transport measurements through a pair of metallic Coulomb islands coupled in parallel (Chapter 5) show that there is strong electrostatic interaction between the islands as they are in close proximity to each other. This capacitive cross talk leads to a rich charge stability diagram.

Nonlocality is a key feature discriminating classical and quantum physics. In chapter 6, we demonstrate a systematic study of the nonlocal electron transport through Aharonov-Bohm (AB) interferometers showing a new aspect of the dynamical nonlocality in a quantum network. Our experimental foundations are supported by a theoretical model that explains the fundamental nature of the dynamical delocalization. Dynamical nonlocality is not limited by the diffusive transport regime or by the specific wave-particle used and damps away with the reduction of the amount of conduction channels.

Finally, in chapter 7, we demonstrate an evidence of coherent charge transport through a1,8-alkanedithiol monolayer embedded as molecular barrier in a system of a pair of Coulomb islands coupled in parallel and working as two parallel SETs. Understanding to what extent transport through organic molecular monolayers is coherent and how the coherence depends on the molecule’s characteristics and/or external parameters is a fascinating question raised in recent years due to the potential application of molecular monolayers in nanoelectronics.

Ksenia S. Makarenko
Enschede, May 2015
Samenvatting

Ladingstransport in “Bottom-Up” Inorganische-Organische en Kwantum-Coherente Nano-Structuren

Dit proefschrift is gebaseerd op resultaten die verkregen zijn uit experimenten ontworpen voor het bestuderen van ladingstransport in “bottom-up” inorganische-organische en kwantum-coherente nano-structuren. Nieuwe onconventionele manieren om elementen van een elektrisch circuit te maken (zoals diëlektroforese, "wedging transfer" en bottom-up fabricage waarbij gebruik gemaakt wordt van selectieve chemische interacties) werden bestudeerd en worden gepresenteerd in dit proefschrift. We onderzochten ook stappen in het begrijpen van fundamentele fysische verschijnselen zoals ladingstransport door een tweetal parallel geschakelde metalen Coulomb eilanden, coherent ladingstransport door organische moleculaire monolagen en dynamische non-lokaliteit in metalen.

Diëlektroforese ("dielectrophoresis", DEP) en wedging transfer zijn top-down technieken die soft-contact van elektroden onder zelf geassembleerde moleculaire monolagen (SAMs) toelaten zonder deze lagen te beschadigen, wat leidt tot de formatie van ~1-2 nm brede moleculaire tunnelcontacten zonder de noodzaak voor extreem smalle nano-kanalen. DEP is een simpele en reproduceerbare techniek met een hoog rendement wat het een goed alternatief maakt voor het fabriceren van moleculaire bruggen. Deze methode laat niet alleen het karakteriseren van een groot aantal moleculaire monolagen toe, maar ook de fabricage van single-electron transistors (SETs) door het vangen van enkele nano-deeltjes ("nanoparticles", NPs) (metallisch of halfgeleider) tussen elektrodes en het ontkoppelen van deze NPs via moleculaire barrières. Wedging transfer is een veelbelovend alternatief voor de fabricage van moleculaire juncties op nano- en microschaal. De lage hoeveelheid werkende devices die met wedging transfer gemaakt werden, is een indicatie voor de noodzaak voor verdere verbetering van dit fabricageproces.

De studie van moleculaire SAMs (hoofdstuk 2.3) laat zien dat elektronentransport door alkaandithiolen een typisch voorbeeld is van niet-resonante tunnelling, onafhankelijk van de temperatuur of het magnetische
veld. De moleculaire lengte en de moleculaire compositie hebben een sterke invloed op de geleiding van de moleculaire juncties. Zoals verwacht resulteren de alkaandithiolen in een hogere weerstand dan π-geconjugeerde moleculaire monolagen.

De continue miniaturisatie van silicium transistoren in de afgelopen decennia, die gedreven wordt door wetenschappelijke en technologische innovaties, wordt mogelijk gemaakt door de ontwikkelingen in top-down fabricagemethoden. Echter, het benaderen van afmetingen onder de ~10 nm maakt top-down methodes moeilijker en duurder. Dit motiveert onderzoek naar nieuwe onconventionele manieren voor het realiseren van functionele nano-elektrische componenten. In hoofdstuk 4 wordt een bottom-up benadering voor de productie van SETs op basis van enkele ~20 nm Au NP geëxplieerde. Met succes hebben wij zelfassemblage van Au NPs met Au "nanorods" (NRs) gecombineerd met top down lithografie. Elektrische metingen van elektronentransport door de SETs bij lage temperatuur laten een duidelijke signatuur zien van klassieke Coulomb-blokkade. Het fabricageproces heeft een zeer hoge reproduceerbaarheid (>50%) en de SETs zijn stabiel gedurende enkele maanden. De temperatuurs- en grootteafhankelijkheid zijn in goede overeenkomst met de theoretische voorspellingen.

Metingen van het elektronentransport door een paar parallel geschakelde metalen Coulomb eilanden (hoofdstuk 5) laten zien dat er een sterke elektrostatische interactie is tussen de eilanden. Deze capacitive koppeling leidt tot een rijk ladingstransportdiagram.

Niet-lokaliteit is een belangrijk kenmerk voor het onderscheiden van klassieke- en kwantumfysica. In hoofdstuk 6 beschrijven we een systematische studie van het niet-lokale elektronentransport door Aharonov-Bohm (AB) interferometers die een nieuw aspect van de dynamische niet-lokaliteit in een kwantum netwerk laten zien. Onze experimenten worden ondersteund door een theoretisch model dat het fundamentele karakter van de dynamische delokalisatie verklaart. Dynamische niet-lokaliteit wordt niet beperkt door het diffusieve transport of door het specifieke deeltje(-golf) dat wordt gebruikt en vermindert met de hoeveelheid geleidende kanalen.

Tenslotte laten we in hoofdstuk 7 een indicatie zien voor coherent ladingstransport door een 1,8-alkaandithiolmonolaag ingebouwd als een moleculaire barrière in een systeem van een tweetal parallel geschakelde Coulomb eilanden en werkend als twee parallele SETs. In hoeverre transport door organische moleculaire monolagen coherent is en hoe de coherentie afhankelijkheid is van de moleculaire karakteristieken en/of de externe parameters is een fascinerende vraag die opgekomen is in de laatste jaren.
vanwege de mogelijkheid om moleculaire monolagen te gebruiken in nano-elektronica.

Ksenia S. Makarenko
Enschede, May 2015
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This thesis is a result of four years of experimental research on the charge transport in bottom-up inorganic-organic and quantum-coherent nanostructures. For me it was, definitely, four great, wonderful years. The four years of hard and interesting work as well as meeting new people, some of them have changed my life 😊. But it would not be even possible to do this work without my Ph.D. adviser Wilfred G. van der Wiel, who gave me an opportunity to join NanoElectronics group as a Ph.D. researcher on the 1st of April 2011, mentioning that it was not a joke. Wilfred, thank you for being a great guide during last four years. I am thankful to you for being patient and never giving strong suggestions and/or judgments and letting your students come to the right answers and conclusions themselves as well as work independently, motivated by their scientific “hunger” for knowledge. I am very glad that I met you not only as a scientist but also as a person. I hope that I will have many chances in future to ask you “a small question” 😊.

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Ksenia S. Makarenko
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Figure LXXVI. Atomic force microscopy image of a Au Aharonov-Bohm interferometer fabricated on top of the p++Si substrate with thermally grown 35 nm thick SiO$_2$ layer. Interferometer contains a gap functionalised by 1,6-octanediithiol self-assembled monolayer and bridged by 60 nm Au nanoparticles. Image made by Martin Siekman.