



High-performance 90° hybrids based on MMI couplers in Si₃N₄ technology

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ABSTRACT

Low-loss, broadband, and low phase deviation optical 90° hybrids based on 2 × 4 multimode interference couplers are firstly demonstrated using Si₃N₄ on SiO₂ technology. Only a simple traditional design method of MMI based on self-imaging theory and a single-stripe Si₃N₄ waveguide geometry with only one step etching process are utilized. The characterization of the fabricated devices is carried out over a wide spectral window of 1520–1610 nm, showing that the measured phase error is less than 8°, and common-mode rejection ratios (CMRRs) are better than –20 dB. The measured total loss of the fabricated device including a 90° hybrid and a 3-dB coupler is <1 dB in a bandwidth over 80 nm. Our analysis also shows large fabrication tolerance with width of ±0.1 μm or length of ±3 μm.

1. Introduction

Optical 90° hybrids permit maximizing spectral efficiency and receiver sensitivity in higher-order modulation schemes, such as quadrature phase shift keying (QPSK) in coherent detection systems [1]. Low loss, low phase error, high common-mode rejection ratio (CMRR), and broadband operation are required to demodulate the optical signal accurately. Previously, multimode interference (MMI) couplers have been employed to realize high-performance hybrids on several photonic technologies such as the InP [2] and the silicon-on-insulator (SOI) platforms [3]. In these high refractive index contrast platforms, methods based on the optimization of the index-contrast are normally used to avoid the strong phase errors introduced by the high-order modes in the MMI hybrids. Such methods include shallow etched waveguides [4] and subwavelength gratings in the lateral cladding of the MMI region [5]. However, these methods require high-resolution lithography tools and precise control of the dry etching process, resulting in reduced tolerance for dimensional deviation during fabrication. In other approaches, such as using a wedge-shaped MMI hybrid [6] to reduce the mode number in order to eliminate the strong phase error of the high-order modes, the bandwidth is limited. Besides these high refractive index contrast platforms, 90° hybrids in relatively low refractive index contrast polymer (SU-8) platform have shown low-loss and good performance for polarization demultiplexing [7] but the bandwidth and durability of the devices is limited due to the polymer properties.

Silicon nitride (Si₃N₄) has been widely employed recently in *non-linear optics* [8], *bio-sensing* [9] and *microwave photonics* [10] owing to its low propagation loss (<0.1 dB/cm), and large transparency window (400–2350 nm) [11]. Compared to the aforementioned technologies, the Si₃N₄ platform shows a great potential for the realization of low-loss, low phase error, and broadband 90° hybrids based on MMIs due to its moderate index contrast and low propagation loss [12]. In this paper, an optical 90° hybrid on a single-stripe Si₃N₄ platform is presented. The dimensional parameters are first extracted by a 2D mode simulation and further investigated using a 3D finite time different domain (FDTD) method. The Si₃N₄ waveguides are fabricated by a full dry etching process and cladded by SiO₂. The fabricated chips are characterized in a spectral window of 1520–1610 nm. The measured result with optimal design at the MMI length of 270 μm shows losses of below 1 dB for wavelength band larger than 80 nm. The measured phase deviation between the output ports are below 6° in the C-band and within 8° for the whole measured spectral range. CMRRs better than –20 dB have also been demonstrated.

2. Device design

Fig. 1 shows the schematic of the 90° hybrid based on an MMI, where a 200 nm thick Si₃N₄ on an 8 μm thick thermal oxide is employed. The device is designed to work under transverse-electric (TE) polarization. The 90° phase relations of the output locations of the MMI are in accordance with the self-imaging theory [13,14]. To ensure high

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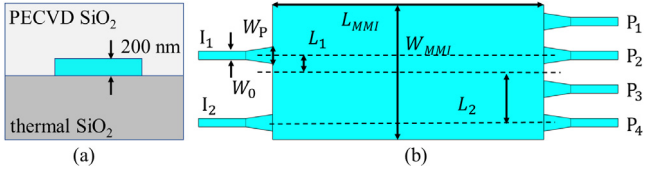


Fig. 1. Schematic of the 90° hybrid: (a) cross-section of the 200 nm thick Si₃N₄ waveguide, and (b) the top-view layout of the device.

quality imaging, the 2 × 4 MMI has to demonstrate low phase errors for the modes, especially the higher-order modes. Additionally, adequate space between the input/output ports is required to reduce the mutual crosstalk. Thus, the MMI width should not be too small. Although a larger MMI width may lead to lower loss and lower phase errors of the device, it results in larger dimensions. With an overall balanced consideration for the loss, phase error and size, we choose the MMI width as $W_{MMI} = 16 \mu\text{m}$, at which the MMI supports 10 TE modes.

The 2D mode simulations are carried out using the commercial suite Optodesigner (Phoenix B.V.). The refractive indices of Si₃N₄ and SiO₂ utilized are 1.984 and 1.446 respectively at 1550 nm. The calculated phase error of the highest order (10th) mode, i.e., the difference between the simulated phase change after fourfold imaging distance propagation and the ideal parabolic phase relations of different modes shown in [13], is ~48°, which is comparable to the phase error obtained in SOI (i.e., ~58°) by the shallow etching technique [4], indicating that the 200 nm thick Si₃N₄ platform intrinsically has lower phase errors. In Fig. 1, the distances of the input port I_1 and output ports P_2 and P_3 to the center of the MMI are chosen to be 2 μm and labeled L_1 . Meanwhile, other distances between the input port I_2 and the output ports P_1 and P_4 to the center of MMI are selected to be 6 μm and denoted as L_2 . The widths of the input/output ports are optimized to $W_p = 3 \mu\text{m}$, following the approach presented in the work of [14] and are linearly tapered to $W_0 = 1.2 \mu\text{m}$ using adiabatic tapers with a length of 15 μm, which avoids the excitation of unwanted higher-order modes. With these parameters, the cross-talks are found to be negligible at the output ports due to sufficient separation distance (i.e., 4 μm).

The performance of the device based on the full 3D structure is calculated using 3D FDTD over a wide spectral range of 1520–1580 nm. For simplicity, the aforementioned refractive indices at a wavelength of 1550 nm are employed in the simulation.

Firstly, an MMI width of 16 μm is studied in 3D FDTD. The MMI length (L_{MMI}) is chosen to be 270 μm, which is equal to three-quarters of the beat length at the wavelength of 1550 nm ($3L_{\pi}/4$). At this length, the excess losses of the hybrid, as shown in Fig. 2(a), are 0.13 dB at 1550 nm and below 0.21 dB for the entire C-band (i.e., 1530–1565 nm). The loss gradually rises as the wavelength increases over 1550 nm. This is because the MMI length is no longer optimal due to the variation of the corresponding effective refractive indices of the modes in the MMI region caused by the wavelength change.

The hybrid phase deviations of the output ports referring to the output port 3 are calculated as $\Delta\phi_{13} = \phi_1 - \phi_3 - 90^\circ$, $\Delta\phi_{23} = \phi_2 - \phi_3 - 180^\circ$ and $\Delta\phi_{34} = \phi_3 - \phi_4 - 90^\circ$, where $\phi_{i,j}$ is the phase of the output port i or j , and $i, j = 1, 2, 3, 4$ indicate different output ports. It can be seen from Fig. 2(b) that all the phase deviations are within 5° in the investigated spectral range for the hybrid, indicating strong broadband properties of the hybrid.

Additionally, the common mode rejection ratios (CMRR) quantitatively imply the relative weakness of the power detected by a pair of balanced photo-detectors [15]. Both CMRRs between in-phase channels (I), i.e., P_1 and P_4 , and quadrature channels (Q), i.e., P_2 and P_3 , are calculated as $20 \log[(P_i - P_j)/(P_i + P_j)]$, where $P_{i,j}$ is the power of the output port i or j . Fig. 2(c) and (d) show the calculated values of CMRRs for the input ports 1 and 2, respectively. The CMRRs are better than -20 dB, resulting in a good power balance between both in-phase and quadrature channels, meaning the hybrid is qualified for operation as a coherent optical receiver. Additionally, it can be seen that there are some dips in the CMRR curves. The power of the corresponding two output ports are equal at the wavelength of dip position, and thus the corresponding CMRR drops to zero according to its definition.

The influence of the variation of dimensional parameters of the MMI on the hybrid performance are studied. In particular, the width variation originating from the fabrication deviation using standard lithography (<0.2 μm) leads to changes in the effective refractive indices of the modes in the MMI, which significantly affects the phases of

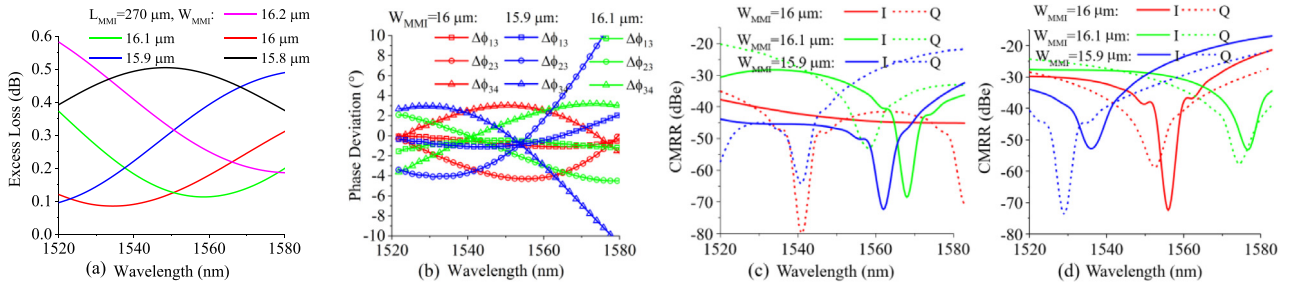


Fig. 2. Parameters of the hybrid at different MMI widths with a fixed MMI length of 270 μm: (a) calculated hybrid loss, (b) the phase deviations between different output ports, (c) the CMRRs of in-phase and quadrature channels with input port 1, and (d) the CMRRs with input port 2.

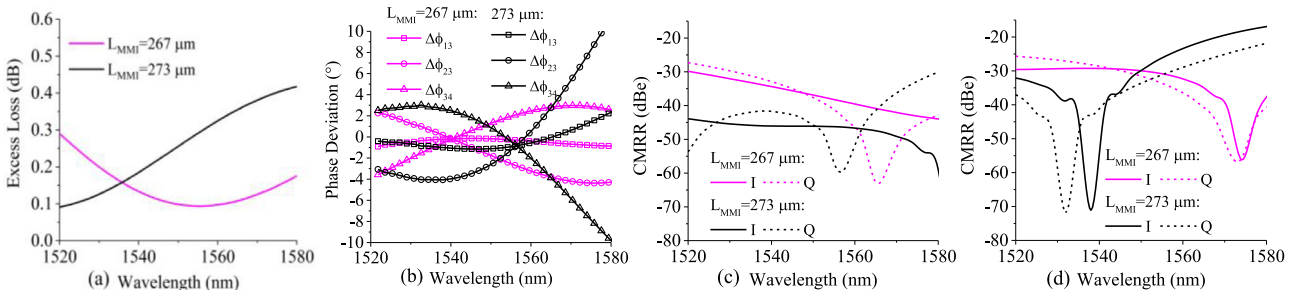


Fig. 3. Parameters of the hybrid at different MMI lengths with a fixed MMI width of 16 μm: (a) Calculated hybrid loss, (b) the phase deviations between different output ports, (c) the CMRRs of in-phase and quadrature channels with input port 1, and (d) the CMRRs with input port 2.

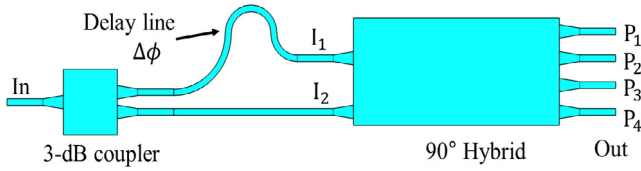


Fig. 4. Schematic of the 3-dB coupler integrated hybrid.

the modes at the output ports after propagation as well as their imaging patterns. Fig. 2(a) also shows the losses considering a variation of the width of the MMI from 15.8 μm to 16.2 μm . With the increase of the deviation from the nominal 16 μm , the loss curve in the C-band rises, indicating that the hybrid is sensitive to the MMI width and a precise control of the width is required during the lithography step. Hence, for the phase deviation and CMRR, an MMI with widths of 15.9 μm and 16.1 μm at a length of 270 μm , where the minimum of the loss shifts to wavelengths of 1520 nm and 1560 nm, respectively, is considered for the width tolerance study, as shown in Fig. 2(b)–(d). The phase deviation $\Delta\phi_{13}$ remains stable with the variation of the MMI width. The deviations $\Delta\phi_{23}$ and $\Delta\phi_{34}$ at the width of 16.1 μm still remain within 5°. However, they rise considerably after a wavelength of 1560 nm at a width of 15.9 μm . The CMRRs for both in-phase and quadrature channels at the width of 16.1 μm are still better than -20 dB, while one of the in-phase channels with input port 2 fails for an MMI width of 15.9 μm .

The beat length change is found to be about 4.5 μm for a 0.1 μm variation of the MMI width, according to 2D mode solver calculations, which requires the length of MMI hybrid to be varied about 3.4 μm (i.e., three-quarters of beat length) in the design in order to compensate for width variation. Therefore, the parameters of the hybrids with the MMI length of 267 μm and 273 μm for the nominal MMI width of 16 μm are simulated by 3D FDTD, and are shown in Fig. 3(a)–(d). As expected, for MMI lengths of 267 μm and 273 μm , the tendencies of the loss and phase deviations as a function of wavelength are similar to those of MMIs of widths 16.1 μm and 15.9 μm [Figs. 2(a) and 2(b)], respectively and nominal length of 270 μm . Except for the in-phase channel CMRR at the length of 273 μm with input port 2, CMRRs better than -20 dB over the investigated spectral window have been simulated. For a thickness tolerance of ± 2 nm, which can be achieved by the state-of-the-art deposition technology, the influence of the thickness variation to the simulated performance is very small, which can be negligible.

3. Experiment results

A single-stripe layer of Si_3N_4 was deposited by low pressure chemical vapor deposition (LPCVD) on thermally oxidized silicon wafers with 8 μm thick silicon dioxide. The fabrication of the Si_3N_4 waveguides follows the process flow presented in [16] by using standard optical lithography (EVG620) and plasma etching (Adixen AMS100). After

fabricating the waveguides, a layer of SiO_2 with ~ 6 μm thick was deposited on top of the device by plasma enhanced chemical vapor deposition (PECVD) to serve as top cladding.

In the fabricated chip, a 3-dB power splitting coupler is integrated for testing purposes, as shown in Fig. 4. The coupler has a width of 5 μm and a length of 15 μm , which is equal to $3L_\pi/8$. Its input and output ports are linearly tapered from 2 μm to 1.2 μm with a taper length of 15 μm . Its excess loss is calculated to be 0.2 dB. The purpose of using this coupler is to form a Mach-Zehnder interferometer (MZI) with the hybrid, where the arm connected to input port 1 has an additional length that introduces a phase delay of $\Delta\phi$ with respect to the arm connected to input port 2. Therefore, a wavelength-dependent phase shift can be obtained between the hybrid input ports, which allows for extraction of the phase deviations between the output ports through characteristic filter transmission curves by directly scanning the wavelength.

In the characterization setup, a laser tunable from 1520 nm to 1610 nm (Agilent 81940A) is used. Single-mode fibers with a mode size of ~ 10 μm and inverse tapers on Si_3N_4 chip are employed for the light input and output. The transmission spectrum of each output port is measured for the full spectral window. A neighboring straight waveguide with the same width (2 μm) is used as a reference waveguide. Fig. 5(a) shows the measured spectra of the 90° hybrid with the MMI length of 270 μm in the range of, as an example, 1545–1555 nm. The high extinction ratios (>20 dB) are due to the perfect imaging in Si_3N_4 hybrid and the uniform power splitting ratio ($50 \pm 3: 50 \pm 3$ over the measured spectral range) in 3-dB coupler.

The total loss, which includes the loss of the hybrid and the loss of the 3-dB coupler, is extracted by subtracting the maximum values of the measured spectrum to the one of the reference straight waveguide, where the effect of the coupling losses and most of the Si_3N_4 propagation losses are eliminated. Moreover, the influence of the propagation losses of the Si_3N_4 waveguide is neglected due to its low loss (measured to be ~ 0.14 dB/cm at 1550 nm). Fig. 5(b) shows the extracted total losses for the MMI lengths of 270 μm and 273 μm . Due to a defect at one of the output ports on the fabricated chip, the results of the hybrid at an MMI length of 267 μm are not shown here. It can be seen that the total loss (i.e., 90° hybrid and 3 dB coupler) at the MMI length of 270 μm is below 1 dB over an 80 nm bandwidth.

The peaks/valleys in each measured spectrum of Fig. 5(a) are separated by the free spectral range (FSR) due to the delay line of the MZI. Each period represents a 2π phase shift. The wavelength separation ($\Delta\lambda$) between the minima of the spectra of output ports i and j relates to the phase deviation $\Delta\phi_{i,j}$, which can be expressed as $\Delta\phi_{i,j} = 2\pi\Delta\lambda/\text{FSR}$ (Fig. 6). In the spectral window considered in this work, the phase deviations of the output ports or an MMI 270 μm long are all found within 6° in the C-band and within 8° over an 80 nm bandwidth. Additionally, the hybrid with an MMI length of 273 μm has a higher phase deviation. An increasing trend can be found when the wavelength is larger than 1570 nm. The CMRRs of in-phase and quadratic channels of the fabricated device are also obtained from the measured peaks of

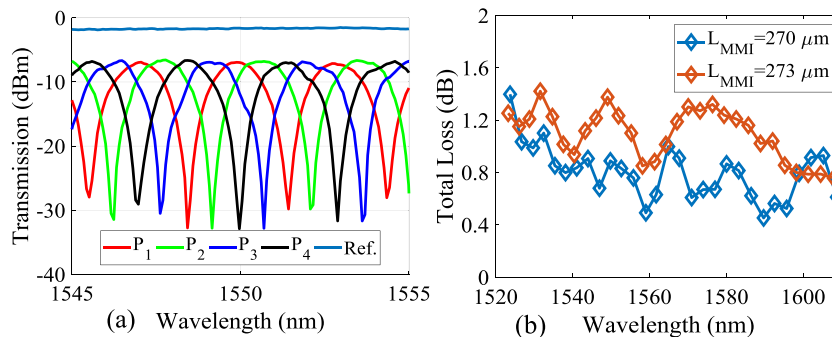


Fig. 5. (a) Measured transmission spectra of the MMI hybrid and reference waveguide. (b) The total loss of the 3-dB coupler integrated MMI hybrid.

Table 1
A comparison of 90° Hybrids.

	Total loss/dB	Phase deviation/°	CMRR/dBe	BW/nm	MMI Size/ μm^2	Technology	Fabrication tolerance
[2]	<1	<5	<-20	94	12 × 360	GalnAsP/InP, 2 × 4 MMI + Phase Shifter + 2 × 2 MMI	-
[4]	-	<5	<-20	50	7.7 × 115.5	SOI, shallowly etched MMI	-
[5]	-	<10	<-20	60	10 × 186.5	SOI, MMI with subwavelength structures	-
[6]	<1	<5	<-20	40	12 × 107	SOI, wedge-shaped MMI	-
This work	<1	<8	<-20	80	16 × 270	Si ₃ N ₄ , traditional simple MMI	±0.1 μm in width

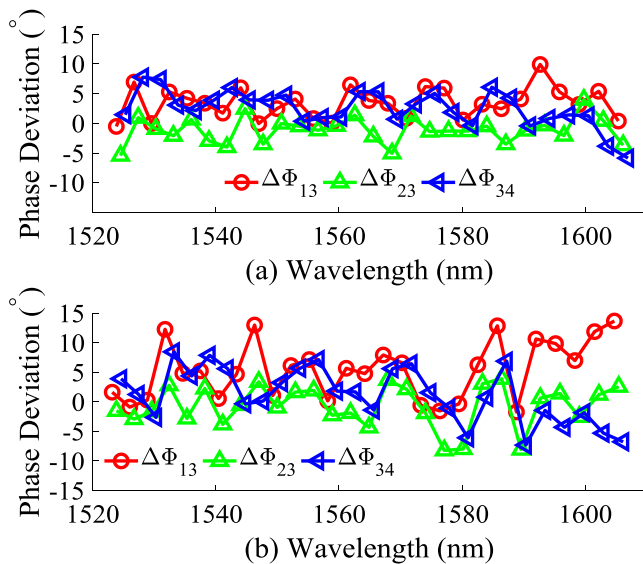


Fig. 6. The phase deviations between the output ports referring to the output port 3 at the MMI length of 270 μm (a) and 273 μm (b).

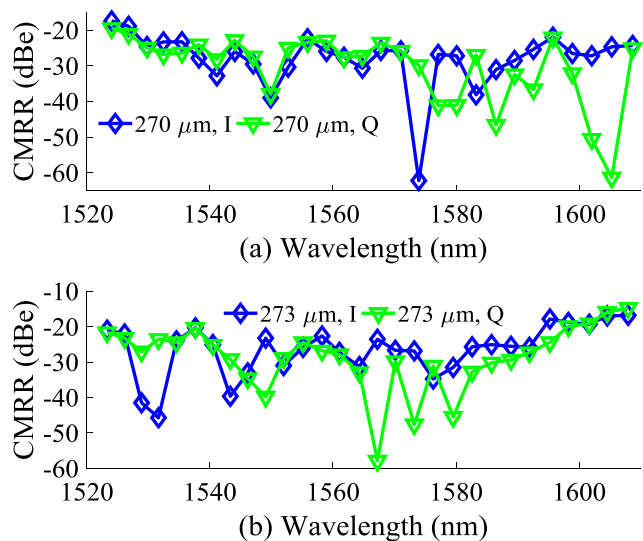


Fig. 7. The CMRRs of the 3-dB coupler integrated MMI hybrid at the MMI length of 270 μm (a) and 273 μm (b).

the spectra by calculating using aforementioned formula in the design part. In Fig. 7, the CMRRs of the hybrids at both MMI lengths are shown. For the hybrid with the nominal length of 270 μm , CMRRs better than -20 dB can be seen in a wavelength range of 1525–1610 nm, indicating broadband operation with good power balance between the

output channels. Also, less than -20 dB CMRRs are also achieved for the hybrid with an MMI length of 273 μm in the range of 1520–1600 nm. We compare our results with other typical works published before, as shown in Table 1. Our work has the advantages of e.g. simple design, only simple etching process required, and large fabrication tolerance while maintaining high performance. The bandwidth is much better than those of the other works except [2], where a more complicated and longer structure consisting of 2 cascaded MMI structures and a phase shifter was used.

4. Conclusion

Optical 90° hybrids in Si₃N₄ technology have been proposed and demonstrated on a 200 nm thick single-stripe layer of Si₃N₄. The hybrids have been designed using an approach that combines a 2D mode solver and 3D FDTD simulations. The influence of the variation of the hybrid dimensional parameters on the device performance has been analyzed. The designed hybrids exhibit excellent performance. The fabricated devices have been integrated on chip with 3-dB couplers and experimentally demonstrated in a spectral window of 1520–1610 nm, showing less than 1 dB total losses, within 8° phase errors between the output ports, and better than -20 dB common mode rejection ratios over an 80 nm bandwidth.

Declaration of competing interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

CRediT authorship contribution statement

Jia Yu: Validation, Formal analysis, Investigation, Writing - original draft. **Jinfeng Mu:** Methodology, Validation, Data curation, Writing - original draft. **Kaixuan Chen:** Methodology, Project administration, Writing - review & editing. **Michiel de Goede:** Validation. **Meindert Dijkstra:** Validation. **Sailing He:** Conceptualization, Supervision, Funding acquisition, Writing - review & editing. **Sonia M. García-Blanco:** Supervision, Funding acquisition, Writing - review & editing.

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