Fermi-liquid behavior in the electrical resistivity of K$_3$C$_{60}$ and Rb$_3$C$_{60}$

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We report on the electrical resistivity of K$_3$C$_{60}$ and Rb$_3$C$_{60}$ thin films. These films, grown at elevated temperatures, are highly textured and consist of large single-crystal grains. The films exhibit metallic behavior up to 500 K, with residual resistivities of 1.2 mQ cm. The low-temperature ($T$) resistivity exhibits a $T^2$ dependence. We suggest that it is dominated by electron-electron interactions, and we find quantitative agreement not only with estimates based on the electron density and the bandwidth, but also with other narrow band systems. The electron-phonon interactions become only important for the resistivity above room temperature. The high superconducting transition temperatures are caused by virtual excitations of high-energy phonons, which are not thermally excited at low temperature.

The films were vacuum sublimed in a tube furnace. The C$_{60}$ powder source was in the center of the furnace at $\sim$400°C, and the glass substrate near the end of the furnace at $\sim$200°C. In this way a deposition rate was obtained of about 500 Å/h. After deposition the films were mounted in a glass tube with electrical feedthroughs. After evacuating the tube the minimum resistivity was attained by repetitive doping and anneal cycles at 150°C.

The films were examined with x rays. The linewidths are resolution limited and show that the films are highly textured along the (1 1 1) planes. The electrical resistivity was measured using a Linear Research resistance bridge (LR400), and always found to be Ohmic. Measurements below room temperature (RT) were performed in a liquid-helium dewar containing a 15 T superconducting magnet, and above RT in a tube furnace. The temperature was monitored with calibrated carbon-glass and platinum resistance thermometers, mounted outside the glass tube, which was placed in an isothermal brick can. Since the thermal response of the sample was very slow, the temperature was changed very slowly by a heater mounted on the brass can.

In Fig. 1 we show the electrical resistivity of K$_3$C$_{60}$ and Rb$_3$C$_{60}$ thin films, heating the samples from 4 to 500 K. We studied five K$_3$C$_{60}$ films and three Rb$_3$C$_{60}$ films. The typical resistivity at RT is 2 mQ cm. Cooling down to the superconducting transition results in residual resistivity ratios between 1 and 2. Our best films have a residual resistivity of 1.2 mQ cm for both K$_3$C$_{60}$ and Rb$_3$C$_{60}$. We note that due to the slow thermal response of our system, the samples were quickly cooled to liquid helium and then slowly heated to RT, while recording the resis-

Electrical resistivity measurements have provided a wealth of information on the conduction mechanism and Fermi-surface properties of organic conductors. From the temperature and magnetic-field dependence of the resistivity the scattering mechanisms can be derived, and for clean samples the Fermi surface can be mapped. For alkali-doped C$_{60}$ the situation seems to be more complicated and even for "optimally" doped samples with stoichiometry near $A_3$C$_{60}$ ($A =$alkali metal) the resistivity is only slightly smaller than the value at the metal-to-insulator boundary. These high resistivities have thus far precluded transport studies of Fermi-surface properties and, moreover, it is not clear what mechanisms are responsible for limiting the conductivity. Our interest in the conductivity stems from the fact that the inelastic-scattering mechanisms causing electrical resistivity are usually identical to the interactions leading to superconductivity.

To study intrinsic electrical transport properties of doped C$_{60}$, we have made metallic thin films, exhibiting normal-state resistivities that are at least as good as reported for the best single crystals. Using thin films we have excellent control of the geometry and obtain homogeneous doping through the film, avoiding problems usual for single crystals. Our earlier K$_3$C$_{60}$ films exhibited granular behavior, and the grain size was found to determine the electrical transport behavior. Therefore, we modified our growth procedure to one that yields large grains and metallic resistivities with a typical residual resistivity ratio of $\rho(RT)/\rho(T_c) \sim 2$. Surprisingly, these metallic films have a resistivity at room temperature of $\sim 2$ mQ cm, which is similar to the values of the granular films which exhibited a negative temperature coefficient $d\rho/dT$. However, near $T_c$ the resistivities of these two types of films are different by a factor of 3, which is reflected in a smaller value of the upper critical field slope.

In this article we will discuss the strong electron scattering in $A_3$C$_{60}$. We argue that the low-temperature resistivity is dominated by electron-electron interactions, and find quantitative agreement not only with estimates based on the electron density and the bandwidth, but also with other narrow-band systems. The electron-phonon interactions become only important for the resistivity above room temperature. The high superconducting transition temperatures are caused by virtual excitations of high-energy phonons, which are not thermally excited at low temperature.

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of the transition at a rate of 2.65 T/K for K$_3$C$_{60}$ and 3.5 T/K for Rb$_3$C$_{60}$. In this Rb$_3$C$_{60}$ film evidence for weak links is seen in the resistance “foot” of the transition.\(^9\)

In discussing these materials we will focus on two aspects of our measurements, namely the magnitude and the temperature dependence of the electrical resistivity. We will use measurements on other conductors as a reference for our observations. The residual resistivity of 1.2 m\(\Omega\) cm for the present films is at least as good as reported for the best single crystals.\(^6\) Slightly smaller values of the resistivity were inferred from reflectivity measurements,\(^10\) but this difference can be associated with the nonspecular surface of the powder samples, and the resulting error in the determination of the absolute value of the conductivity.

The question can be raised whether the resistivity is intrinsic or due to geometric factors which give rise to a tortuous current path. From the upper critical field slopes we derive Ginzburg-Landau coherence lengths of 31 and 22 Å for K$_3$C$_{60}$ and Rb$_3$C$_{60}$ respectively. Since the Pippard coherence length can be estimated from the band structure to be \(\xi_0 \approx 140\) Å, we are in the dirty limit. In this case the upper critical field slope is given by\(^11\)

\[
-dH_{c2}/dT\big|_{T=\gamma_c} = 4780\gamma p_0
\]

with \(\gamma\) the renormalized linear specific-heat coefficient and \(p_0\) the residual resistivity. Thus, we can use the upper critical field slope as a direct measure of the intrinsic value of the resistivity on the length scale of the pair-breaking process \((\sim \xi)\). Using appropriate estimates for \(\gamma\) (see below), we find that the measured values of the resistivities are indeed intrinsic and thus relevant to the pair-breaking process, and also for superconductivity.

It is of paramount importance to establish whether the low-temperature conductivity in \(A_3C_{60}\) is in keeping with a Fermi-liquid description. A resistivity of 1 m\(\Omega\) cm is for most materials above the Mott limit, and would render them insulating. Therefore, we will first determine the Mott limit for this material. For a Fermi-liquid description to be appropriate, it requires that \(k_F l > 1/2\pi\), with \(k_F\) the Fermi wave vector, and \(l\) the mean free path at zero temperature averaged over the Fermi surface.\(^12\) We establish \(k_F l\) by using the general relation between the conductivity and the Fermi-surface area \(S_F\), assuming an isotropic mean free path: \(^12\)

\[
\sigma = \frac{\epsilon^2}{\hbar} \frac{1}{12\pi^3} (S_F l) \text{.}
\]

Although the Fermi surface is not known in detail, one may crudely estimate \(k_F l\) in two limiting cases. One is the single noninteracting band with three carriers per C$_{60}$ molecule. Combined with the experimental residual resistivity of 1.2 m\(\Omega\) cm, this yields \(k_F l \approx 2.5\) as an upper bound for the mean free path at low temperatures. If there were three degenerate parabolic bands (derived from the \(t_{1u}\) orbitals), we would obtain \(k_F l \approx 12.5\). In either case the conductivity is somewhat larger than the characteristic conductivity scale: \(^12\)

\[
\sigma_{\text{mott}} = 0.01\epsilon^2 k_F /\hbar \text{,}
\]

FIG. 1. Temperature dependence of the electrical resistivity of K$_3$C$_{60}$ and Rb$_3$C$_{60}$ thin films between 4 and 500 K. The solid line through the data of Rb$_3$C$_{60}$ between 50 and 250 K is a fit including both electron-electron and electron-phonon interactions.

We show in Fig. 2 the behavior near the superconducting transition of K$_3$C$_{60}$ and Rb$_3$C$_{60}$ films. The transition is very sharp with the 10–90% width of the transition \(~1\) K. Applying a field up to 12.5 T shifts the midpoint

FIG. 2. Temperature dependence of the electrical resistivity of K$_3$C$_{60}$ and Rb$_3$C$_{60}$ near the superconducting transition in magnetic fields of 0, 1, 2.5, 5, 7.5, 10, 12.5, and 15 T. The magnetic field was oriented perpendicular to the current direction.
which we estimate to be in the range $0.5-0.7$ (mΩ cm)$^{-1}$ depending on the assumed $k_F$. Thus a *Fermi-liquid description of the metallic state is appropriate*. The Mott limit for $A_3C_{60}$ is smaller than in regular metals because of the low conduction-electron density.

In the three-dimensional Bloch-Gruneisen model, the acoustic phonons give rise to a $T^3$ temperature dependence, whereas electron-electron Umklapp scattering results in a $T^2$ behavior. Our data on Rb$_2$C$_{60}$ exhibit a temperature dependence that can be accurately fitted between 50 and 200 K with $A \cdot T^2 + B \cdot T^3$, with a coefficient $A = 10^{-2}$ μΩ cm/K$^2$ and $B = 3.6 \times 10^{-5}$ μΩ cm/K$^3$, as shown in Fig. 3. We can make theoretical estimates of both parameters to see what values can be expected for $A_3C_{60}$. The electronic $T^2$ coefficient $A$ can be estimated from

$$A \sim \frac{1}{\omega_p^2 \tau_0} \frac{1}{T_F^2}$$  \hspace{1cm} (4)

with $\tau_0^{-1}$ the bare scattering rate, and $\omega_p$ the plasma frequency. $\omega_p$ depends only on the electron density and is roughly 1 eV.$^{13}$ The scattering rate can be estimated from Coulomb interactions of an electron gas with an average separation between the electrons of $a_L$: $\hbar/\tau_0 \approx e^2/a_L = (a_0/a_L) \times 27$ eV, with $a_0$ the Bohr radius. This yields $\tau_0 \approx 1$ eV. Using a Fermi temperature $T_F \approx 1500-2000$ K, based on susceptibility measurements$^{14}$ we find that $A \sim 1-2 \times 10^{-2}$ μΩ cm. Thus the magnitude of the $T^2$ term is consistent with a simple estimate of the electronic scattering.

The electron-phonon contribution to the resistivity was calculated, and estimated to be 69 μΩ cm at 260 K.$^{15}$ Other calculations obtained 160 μΩ cm at 260 K.$^6$ Both estimates are an order of magnitude smaller than the experimentally observed increase between $T_c$ and 260 K, supporting our view that the low-temperature resistivity is dominated by electron-electron interactions. Conversely, if one interprets the resistivity with electron-phonon scattering, unreasonably large values of the coupling constant $\lambda > 1$ are required.$^8$ However, it is thought that the pairing mechanism for superconductivity is due to electron-phonon interactions,$^{16}$ and usually, the interactions leading to resistivity are identical to those leading to superconductivity. However, in $A_3C_{60}$ the phonons with a large coupling to the electrons have been attributed to two optical modes with energies above 1000 K.$^{16}$ These high-frequency phonons mediate superconductivity via virtual excitations, but these vibrational states will not be appreciably populated under the conditions of our experiment. Of course, the high-frequency virtual phonons can induce changes in the magnitude of the $T^2$ resistivity by moderating the effective *el-el* interaction.$^{17}$

Equation (4) was confirmed for many materials$^{18}$ by relating the resistivity coefficient $A$ to $\gamma$, the linear specific-heat coefficient, which is linear with $T_F^{-1}$ (see Fig. 4). All narrow-band systems fall on one line with slope 2. The transition metals have the same slope but a different proportionality factor. For $A_3C_{60}$ we can estimate $\gamma$ from the specific-heat jump at $T_c$, which results in a value of 48 mJ/mol K$^2$. This puts Rb$_2$C$_{60}$ on the line for narrow-band systems. Of course, the origin of the narrow band is different for the various materials, arising here from the small wave-function overlap. Using literature values,$^{19}$ we note that intercalated graphite KC$_8$ also falls on this line, even though $\gamma$ is an order of magnitude smaller. KC$_8$ is similar to $A_3C_{60}$ in that superconductivity is mediated by high-frequency optical phonons. However, it should be pointed out that in two-dimensional materials the resistivity due to acoustic phonons also gives rise to a $T^2$ dependence. In KC$_8$ the resistivity can be totally accounted for by *el-el* interactions, given its value of $\gamma$. For other two-dimensional organic superconductors,$^{20}$ the ET-salts, the resistivity coefficient $A$ is far larger than expected from the Fermi temperature, and

FIG. 3. Temperature dependence of the electrical resistivity of (a) crystalline Rb$_2$C$_{60}$, (b) granular K$_3$C$_{60}$, and (c) underdoped granular K$_x$C$_{60}$ (x < 3) thin films.

FIG. 4. Resistivity coefficient $A$ vs linear specific-heat coefficient $\gamma$ for wide- and narrow-band conductors. The line through the heavy fermion compounds and the 415 compounds corresponds to $A/\gamma^2 = 1 \times 10^{-2}$, and includes Rb$_2$C$_{60}$ and KC$_8$. The line through the transition metals corresponds to $A/\gamma^2 = 0.4 \times 10^{-6}$. The traditional organic superconductors have much larger ratio's $A/\gamma^2$. 

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*Note:* The above text contains a mix of scientific notation, references, and complex mathematical expressions. It is a transcription of a scientific document that discusses the properties of superconducting materials, focusing on the resistivity and electron-phonon interactions. The text includes theoretical estimations and experimental results, along with references to other works for further reading.
the resistivity seems to be dominated by phonons. This strongly suggests that superconductivity in the conventional organic conductors is also mediated by electron-phonon interactions.

Thus we suggest the following picture for the temperature-dependent transport properties. Usually, in charge-transfer conductors the electrical conductivity is thought to be dominated by the charge-transfer integral between adjacent molecules, resulting in a bandwidth that should be compared with the on-site Coulomb repulsion. However if we take the Fermi-surface area for K$_3$C$_{60}$ (2.4 × 10$^{16}$ cm$^{-2}$) from the band-structure calculation by Erwin$^{21}$ and solve Eq. (1), we obtain a mean free path, $l = 5$ Å. Thus the mean free path is smaller than the size of a C$_{60}$ molecule and the temperature-dependent scattering is taking place on the C$_{60}$ molecule. If we take the radius of the C$_{60}$ molecule as 3.5 Å then the circumference of the molecule is 22 Å, this allows the three conduction electrons to be placed on the molecule with a 7-Å separation, in good agreement with the mean-free-path estimate. This crude model has analogy with a previous picture developed to explain the delayed ionization of C$_{60}$ in terms of the annihilation of multiple excitons which migrate over the surface of the molecule. $^{22}$

In conclusion, we have studied crystalline films of K$_3$C$_{60}$ and Rb$_3$C$_{60}$. The films exhibit sharp superconducting transitions and metallic behavior up to 500 K, with a residual resistivity of 1.2 mΩ cm. The films are in the dirty limit with mean free paths comparable to the size of a C$_{60}$ molecule. The resistivity is smaller than the Mott limit, and thus a Fermi-liquid description is appropriate. The parameters describing the transport data are consistent with an electron-electron scattering mechanism, which is large because the bandwidth is narrow.

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22. Degiorgi et al. calculate a much larger mean free path of about 45 Å, which would become 180 Å for a more reasonable value for the Fermi velocity. However, their model assumes that less than 1% of the carriers in the $t_{2g}$ band contributes to the dc conductivity. We assume that all carriers of the $t_{2g}$ band contribute to the conductivity. L. Degiorgi, G. Gruener, P. Wachtet, S.-M. Huang, J. Wiley, R. L. Whetten, R. B. Kaner, K. Holzer, and F. Diederich, Phys. Rev. B 46, 11250 (1992).