Degenerate four-wave mixing with a tunable excimer laser

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We use a simple, forward-geometry degenerate four-wave mixing setup to monitor weak absorptions of various gas-phase molecules with a tunable excimer laser. With this technique, state-selective detection of \( \text{H}_2, \text{CO}, \text{H}_2\text{O}, \) and \( \text{O}_2 \) is demonstrated. The dependence of the forward-geometry degenerate four-wave mixing signals on various experimental parameters (e.g., pressure, laser power) is determined. Several mechanisms for the generation of the observed signals are discussed, including diffraction from density gratings or thermal gratings and two-photon degenerate four-wave mixing.

1. Introduction

Degenerate four-wave mixing (DFWM) has been demonstrated as a sensitive technique to monitor gas-phase species.\(^1\)\(^-\)\(^6\) The technique has been applied to radicals such as OH and NH, in which transitions to electronic states are easily accessible. Here we demonstrate a DFWM experiment that uses a tunable excimer laser to state-selectively detect weak gas-phase transitions in \( \text{H}_2, \text{CO}, \text{H}_2\text{O}, \) and \( \text{O}_2 \). The ability to detect all of these species sensitively makes this technique a promising diagnostic tool for many combustion environments. This technique is one of a host of gas-phase grating experiments that are being developed to measure background-free gas-phase absorptions. Related gas-phase grating-based techniques were recently demonstrated by Buntine et al.\(^7\) and Zhang et al.\(^8\) Buntine’s technique, termed two-color laser-induced grating spectroscopy, uses nondegenerate light pulses and requires multiple resonances in the molecule. This research was recently extended to the study of both two-photon transitions\(^9\) and dissociating molecules.\(^10\) Zhang’s technique is also a double-resonant technique in which an excitation laser precedes a DFWM scheme so that DFWM can be carried out from the excited state.

Earlier DFWM experiments\(^1\)\(^-\)\(^6\) showed the applicability of the DFWM technique in flames and combustion environments. These experiments were done by using the backward-geometry detection scheme. Phase-conjugate mirrors could then be used to maintain the coherence properties of the grating-generating beams, even in turbulent environments. Our forward-geometry detection scheme does not possess this phase-conjugate property. Recent experiments by Fourkas et al.\(^11\) showed that transient grating experiments in flames could be performed with an experimental geometry similar to the one we use.

These DFWM and grating-based techniques complement laser-induced fluorescence, direct absorption, and ionization detection schemes. The techniques are quite sensitive and rely solely on the absorption process; the detected molecules do not have to radiate or ionize in order to be detected. Additionally, the signal comes out as a coherent light beam and can be detected in a zero-background manner in a location remote from the interaction region. Similar techniques have been used to study optical phase conjugation\(^12\)\(^-\)\(^15\) and to detect transient absorptions in liquids.\(^16\),\(^17\)

Here we report the use of a simple, forward-geometry degenerate four-wave mixing (DFWM-FG) arrangement\(^18\),\(^19\) as a way to monitor weak absorptions of stable molecules in the gas phase by using a tunable excimer laser. In particular we demonstrate the detection of \( \text{H}_2 \) by means of the \( E, F \ 1\Sigma_g^+ (v' = 6, 7) \leftarrow X \ 1\Sigma_g^+ (v'' = 0) \) two-photon transition, the detection of CO by means of the one-photon spin-forbidden singlet-triplet transition \( a \ 3\Pi (v' = 2) \leftarrow X \)
with an absorption in the gas sample, then a spatial light. If the wavelength of the beams is resonant periodically varying spatial intensity distribution of the beams, interference of two of the beams creates a focused through a single lens. At the intersection of parallel coherent laser beams. The three beams are located at three corners of a rectangle to define three placed in the excimer laser beam with 2-mm holes
troscopy in the DFWM-FG technique described here
grating picture will be used here. The experimental used picture, in terms of an induced nonlinear polarization
evidence for the generation of density gratings, discussed in Subsection 4.B, supports the choice of the
crossed in a cell containing the sample by being
can be explained both in a nonlinear optics picture, in terms of an induced nonlinear polarization and the third-order susceptibility tensor $\chi(3)$, and in a dynamic grating picture. Both pictures are being used concurrently. For reasons of clarity, the grating picture will be used here. The experimental evidence for the generation of density gratings, discussed in Subsection 4.B, supports the choice of the more elucidating and pedagogical grating picture. The apparatus used for performing the DFWM spectroscopy in the DFWM-FG technique described here is schematically represented in Fig. 1. A mask is placed in the excimer laser beam with 2-mm holes located at three corners of a rectangle to define three parallel coherent laser beams. The three beams are crossed in a cell containing the sample by being focused through a single lens. At the intersection of the beams, interference of two of the beams creates a periodically varying spatial intensity distribution of light. If the wavelength of the beams is resonant with an absorption in the gas sample, then a spatial distribution of excited molecules, a grating, is created. The grating period $\Lambda$, equivalent to the grating fringe spacing, is determined by the wavelength $\lambda_p$ of the coherent laser beams that creates the grating and the crossing angle $\theta$ between the interfering beams$^{15}$:

$$\Lambda = \frac{\lambda_p}{2 \sin(\theta/2)}. \quad (1)$$

A third laser beam of wavelength $\lambda_c$ focused at the interaction region in the cell is diffracted off of the grating. The diffracted beam comes out of the sample toward the fourth corner of the rectangle (behind the focus). The diffraction of the probe beam can be described as a Bragg reflection in which the following condition holds:

$$\sin \alpha = \frac{m \lambda_c}{2 \Lambda} = \frac{m \sin(\theta/2) \lambda_c}{\lambda_p} = m \sin(\theta/2), \quad m = 1, 2, \ldots \quad (2)$$

The deflected beam ($\lambda_c$) is degenerate in wavelength with the two beams setting up the grating ($\lambda_p$), and it is automatically phase matched if the holes in the mask are chosen as described. The crossing angle of the two laser beams that form the grating is $\theta$, the exit angle of the signal beam is $\alpha$, and $m$ is the order of the diffraction. For a thick grating that has a sinusoidal intensity pattern (i.e., one-photon transition and no saturation of the transition), the first-order diffraction ($m = 1$) is the only order that is phase matched and observed. The reflectivity of the grating is determined by the total number of probed grooves, hence by the combination of the groove spacing and the spatial overlap of the beams. For a given geometry of the three input laser beams, a long focal length lens makes a grating with larger groove spacings than a grating created with a shorter focal length lens, because of the shallower crossing angle. If diffusion is the mechanism for destruction of the grating, it will persist longer when formed with the larger groove spacing.

It is important to note that gratings will be set up in the medium by various combinations of the incoming beams. From inspection of Fig. 1, we see that beams 2 and 3 will set up a grating to which beam 1 is phase-matched, and thus part of beam 1 will be deflected through the spatial filter onto the detector. Similarly, beams 1 and 2 will set up a grating off of which part of beam 3 will deflect onto the detector, although the diffraction will not be as strong because of the larger angle of incidence. A third grating, set up by beams 1 and 3, deflects beam 2 at a different angle and is not detected in this geometry. Note that beam 2 takes part in the creation of both of the gratings that are detected.

**2. Degenerate Four-Wave Mixing in Forward Geometry**

DFWM can be explained both in a nonlinear optics picture, in terms of an induced nonlinear polarization and the third-order susceptibility tensor $\chi(3)$, and in a dynamic grating picture. Both pictures are being used concurrently.

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**3. Experimental**

In the DFWM-FG experiments described here, a line-narrowed tunable excimer laser (Lambda Physik, EMG 150 MSCT) is used as the radiation source. Operating on ArF at 193 nm, the laser has a linewidth of approximately 1.0 cm$^{-1}$. The laser is tunable from 51,600 to 51,850 cm$^{-1}$. The ArF laser output energy is approximately 50 mJ per pulse and this energy is homogeneously distributed in a 7 mm x 22 mm rectangular-shaped beam. Running on KrF at 248 nm, the laser has an output of approximately 150 mJ, in a 0.5-cm$^{-1}$ line, tunable from 40,200 to 40,350 cm$^{-1}$. The beam dimensions of the KrF excimer laser are almost identical to those of the ArF laser. The tunable excimer laser has a tuning range of approximately 1 nm, which is an obvious limitation for doing spectroscopy. However, many important
The laser radiation is coherent enough over the beam cross section that three parallel coherent beams can be formed by sending the main laser beam through a mask. The use of unstable resonator optics in the amplifier of the excimer laser is required to generate this coherence. So far, no DFWM-FG signals have been recorded with the laser in the amplified oscillator mode. Most pulsed dye lasers have incoherent properties over their beam cross section. Therefore, when using a dye laser, one can generate a grating most efficiently by splitting the dye laser beam with beam splitters and by focusing the split beams separately. To ensure maximum coherence, one must make sure that each light beam travels the same distance to the crossing region. This again shows an important advantage of the application of tunable excimer lasers with this simple geometry to this field of spectroscopy.

The mask, positioned 5 cm behind the amplifier’s output coupler, consists of three 2.0-mm-diameter holes in an aluminum plate. The holes are located on three corners of a rectangle that has sides of 4.0 and 10.0 mm. The position of the mask in the laser beam is adjusted so that the energy per pulse of the three secondary beams is approximately equal. The energy of the three individual laser beams is 1 mJ per pulse at maximum. In some experiments a stack of two or three masks is used to prevent stray light from the primary excimer laser beam from interfering with the signal beam. The three laser beams are focused with a 50-mm-diameter, 30-cm focal length lens, passing a quartz window of a stainless-steel cell filled at subatmospheric pressures (typically between 10 and 300 mbars) with the gases under investigation.

The signal beam is detected with either a photodiode detector (Lambda Physik, LF 302 UV) or with a photomultiplier tube detector (EMI 9635 QB). The experiments on O$_2$ and H$_2$O are partly performed in room air at a pressure of 1 bar. With H$_2$O in ambient air (typical Dutch humidity), the DFWM-FG signal is intense enough to be traced by eye by means of its blue fluorescence on a piece of white paper, even with the room lights on. The signal from the photodetector is fed into a boxcar integrator, and the 10- or 30-shot averaged output is displayed on a strip-chart recorder. None of the spectra shown here are normalized to laser power.

4. Results and Discussions

A. Molecular Spectra

In the upper panel of Fig. 2, the DFWM-FG spectrum of the spin-forbidden one-photon transition from the $X^1\Sigma^+ (v''=0)$ state to the metastable $a^3\Pi (v'=2)$ state in CO is shown. The assignments of all the individual lines in the spectrum, as well as a simulation of the expected line intensities, are given in Meijer et al. A direct comparison of the observed and theoretically expected line intensities is somewhat difficult. First, a spectral fluctuation in the intensity of the locked (i.e., narrow-band) laser power over the ArF gain profile exists. In addition, near 51,790 cm$^{-1}$, narrow-bandwidth laser operation ceases completely as a result of an intracavity metastable C-atom absorption. Second, some well-known rotational lines in the $v'=4 \rightarrow v''=0$ band of the Schumann–Runge system of O$_2$ absorb the laser light between the laser head and the detector. Nevertheless, a qualitative comparison of the DFWM-FG spectrum shown here with the theoretically predicted spectrum for CO at 300 K (Ref. 22)
shows a reasonable correspondence between observed and calculated line intensities. The CO spectrum shown here has been recorded with 300 mbars of CO in the cell, but even with the photodiode detector the CO spectrum could be measured at pressures down to 10 mbars. At 300 mbars of pressure the spectrum remains optically thin so that the signal beam is not attenuated as it leaves the sample cell.

In the lower panel of Fig. 2, the DFWM-FG spectrum of the two-photon $E, P^1S^+_g (\nu' = 6, 7) \rightarrow X^1S^+_g (\nu'' = 0)$ transition in 50 mbars of H$_2$ is shown. The four lowest $Q$-branch transitions to the $\nu' = 6$ level, as well as the $Q(2)$ transition to the $\nu' = 7$ level, lie within the tuning range of the ArF laser.

A small nonresonant background signal is visible in the spectrum. One possible explanation is that the background is produced by diffraction from a grating of ions produced by a direct near-resonant three-photon ionization of the H$_2$. The dips in this broad signal are due to the absorption of the laser light on its way to the detector by the aforementioned O$_2$ resonances. Spectra similar to the one shown here have been obtained by using either $(2 + 1)$ resonance-enhanced multiphoton ionization (REMPI) with total ioncurrent detection or two-photon excited laser-induced fluorescence.

The question remains as to the mechanism responsible for the observed signal. One possible mechanism is the two-photon analog of the DFWM experiments, which is degenerate eight-wave mixing. This is a high-order process and would therefore be expected to be weak. Because of the strength of the signal and the power dependence that is discussed below, we do not believe that our signal is due to a degenerate eight-wave mixing process. A more likely explanation is that the process producing the signal beam is not from diffraction from a stationary grating but rather from a resonance-enhanced difference-frequency mixing mechanism, in which the resonance occurs at the two-photon step and the output beam is identical in frequency to the input beam. A four-wave mixing signal produced in this manner would be identical to the one observed but would be of lower order and therefore stronger. It should be noted that this process is not described by a grating picture, because the entire medium contributes to the signal. This contribution makes the signal more robust for diagnostic purposes. The signal strength will decay with the collisional dephasing rate but not with the grating diffusion rate. Recently a tunable variant of this mechanism was published in which an excimer laser was used to excite the same two-photon transition in H$_2$, and in which a second tunable laser beam was used to stimulate the emission of a vacuum UV photon.

For H$_2$ a second-order signal beam [$m = 2$ in Eq. (2)] is also visible (i.e., diffracted at twice the incident angle), even at a pressure of 50 mbars. The H$_2$ spectrum measured by this second-order deflection shows more nonlinear line intensities. Although there are several mechanisms that would lead to second-order diffraction, including degenerate six-wave mixing and saturation of the grating, we have no conclusive evidence of the origin of this signal.

We have obtained molecular spectra of O$_2$ and H$_2$O by focusing the three excimer lasers in room air. The O$_2$ DFWM-FG signal is obtained by focusing the 193-nm ArF excimer laser beam in air. The predissociative $B^3\Sigma_u^- (\nu' = 4) \rightarrow X^3\Sigma_g^- (\nu'' = 0)$ Schumann–Runge band transitions of O$_2$ (Ref. 24) are detected. The line intensities in the observed spectrum are somewhat distorted because much of the laser light (including the signal beam) is absorbed by the oxygen resonances in the beam path. Superimposed on the broad $B \rightarrow X$ O$_2$ transitions, unassigned sharp transitions of either O$_2$ or O$_2^+$ are observed. These resonances have also been observed by using laser-induced fluorescence.

Figure 3 shows the spectrum obtained when the KrF (248-nm) excimer laser is scanned over the H$_2$O $C^2\Pi_A \rightarrow X^2\Pi_X$ transition. When excited to the $C ^1B_1$ state, some of the H$_2$O predissociates and thus forms OH in the $A ^2\Sigma^+$ state, and some is ionized to form H$_2$O ions. This H$_2$O transition has been observed and assigned by Meijer et al. by using $(2 + 1)$ REMPI-detecting H$_2$O ions as well as the detection of OH $A ^2\Sigma^+$ state emission as a function of the laser frequency. The transition has also been observed by using the two-photon excited fluorescence of the H$_2$O molecule. Meijer et al. determined the photodynamics of the predissociation, ionization, and fluorescence processes when this state of H$_2$O is excited. The spectrum obtained by monitoring the OH $A ^2\Sigma^+$ state emission as the photolysis laser wavelength is scanned is very different from our DFWM-FG spectra.

![Fig. 3. DFWM-FG spectrum of the H$_2$O $C ^1B_1 \rightarrow X ^1A_1$ transition in ambient air taken with a tunable KrF excimer laser. The peaks are all assigned in Ref. 31.](image-url)
The DFWM-FG spectrum we observe is nearly identical to the aforementioned (2 + 1) REMPI spectrum and the parent molecular fluorescence excitation spectra. One possible explanation is that the grating probed in this experiment is a density grating formed from the difference in the total number of H$_2$O molecules or H$_2$O$^+$ ions. The probed grating is clearly not composed of regular population differences of the OH photoproducts. A more likely explanation is that the process producing the signal beam is the same as that which was hypothesized for the H$_2$ signal, which was resonance-enhanced difference-frequency mixing. We believe that this is a useful way to observe many two-photon transitions.

B. Forward-Geometry Degenerate Four-Wave Mixing Pressure Dependence

To quantify the origin of the observed four-wave mixing processes, we determine the pressure dependencies of the DFWM-FG signals in H$_2$. Figure 4 shows the pressure dependence of the four-wave mixing signal of pure H$_2$. The pressure in the cell is varied between 10 and 200 mbars. The curve in Fig. 4 corresponds to a cubic pressure dependence and fits the data remarkably well. The experiment is repeated for pure CO, for which a cubic pressure dependence is also found. In the CO experiment the pressure is varied from 20 to 550 mbars.

To check the influence of the background pressure on the signal, we fill the cell with 50 mbars of H$_2$. Helium is added as a foreign gas, and the total pressure is varied while we monitor the DFWM-FG signal. The measured dependence is shown in Fig. 5. Here a clear linear behavior is observed, indicating the presence of a collision-induced thermal (or density) grating. A thermal grating is formed by the difference in temperature between where the molecules have been excited and collisionally relaxed and where they have not. The difference in temperature creates a density grating that scatters the probe laser beam. The lowest data point has not been included in the fit because only H$_2$–H$_2$ collisions are relevant at this pressure. From the two experiments above, we conclude that at pressures above approximately 10 Torr a density grating is generated by a collisional process in the sample during the pulse duration of the laser. This density grating is produced by collisional energy transfer from the excited H$_2$; as the pressure increases, the number of collisions increases during the laser pulse, and more energy is transferred into the sample. Additionally, the higher pressure leads to a slower diffusion rate, which maintains the density grating and increases the scattering efficiency.

In the H$_2$ experiments the DFWM signal grows quadratically with the density of the probed molecule, as is the case for four-wave mixing processes such as DFWM and coherent anti-Stokes Raman spectroscopy. However, at the higher pressures of our experiment, we know that part of that enhancement is due to the formation of a density grating. The fact that the signal increases rather than decreases with pressure makes the technique complementary to existing diagnostic techniques, such as laser-induced fluorescence and REMPI, which work better at lower pressure as a result of collisional quenching of the fluorescence and the reduction of the mean-free path of the electrons and ions at atmospheric pressures, respectively. However, this technique must be better characterized before quantitative measurements can be attempted.
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